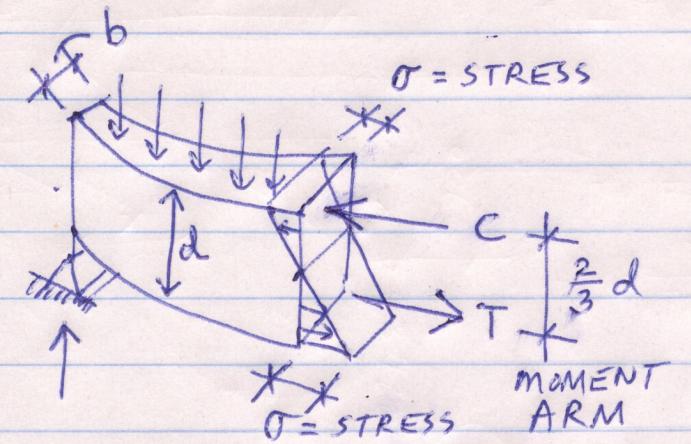
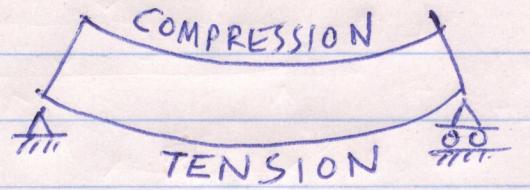
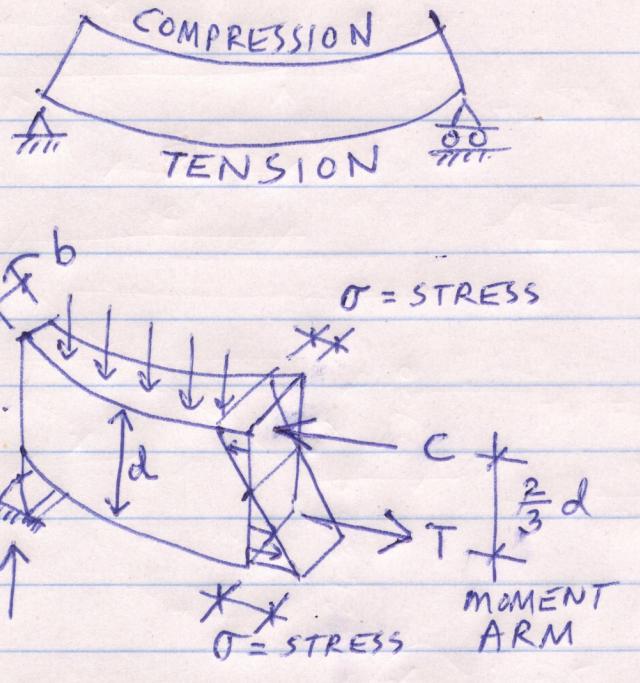


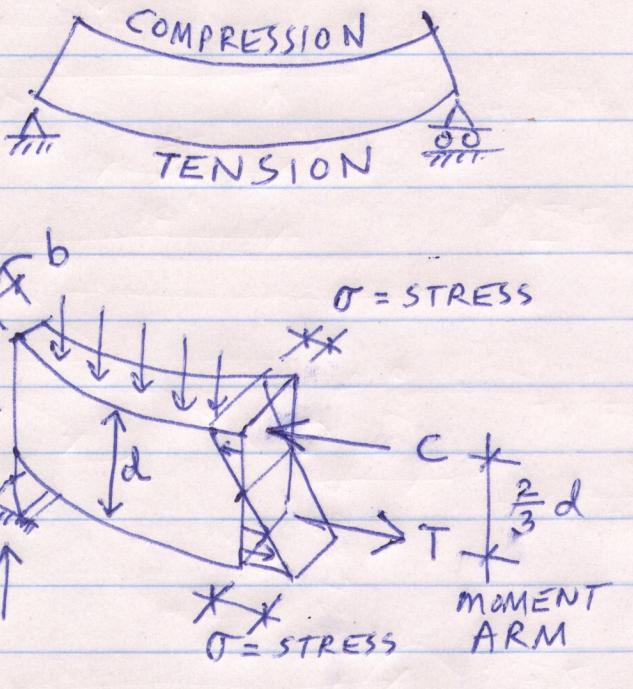
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Steel beams



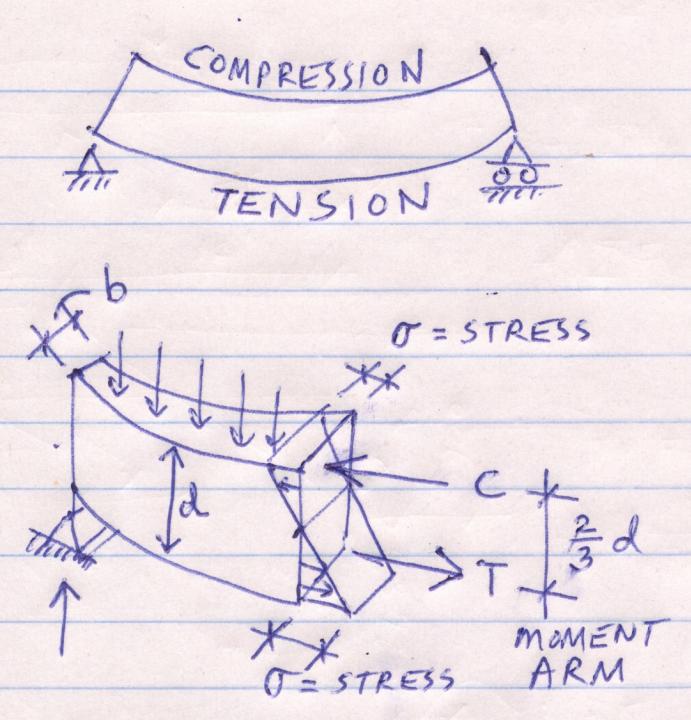


The force couple consisting of the compressive and tensile resultants is what we call the “bending moment” at the section where the free-body diagram is cut: $M = C(2/3)(d)$.



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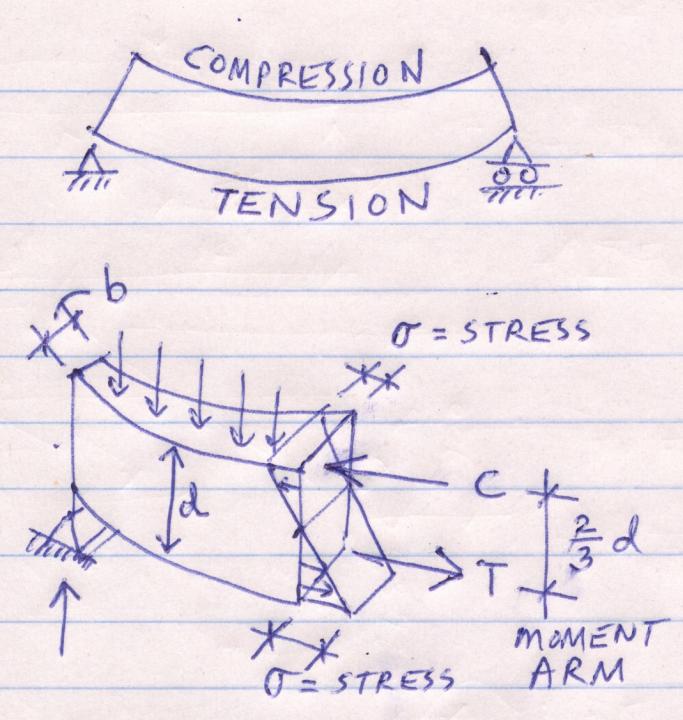
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S_x is called the “section modulus”



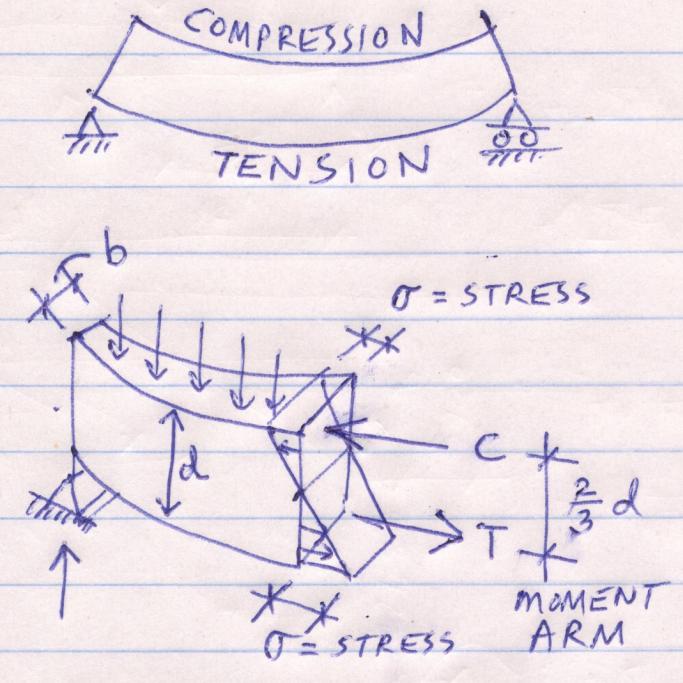
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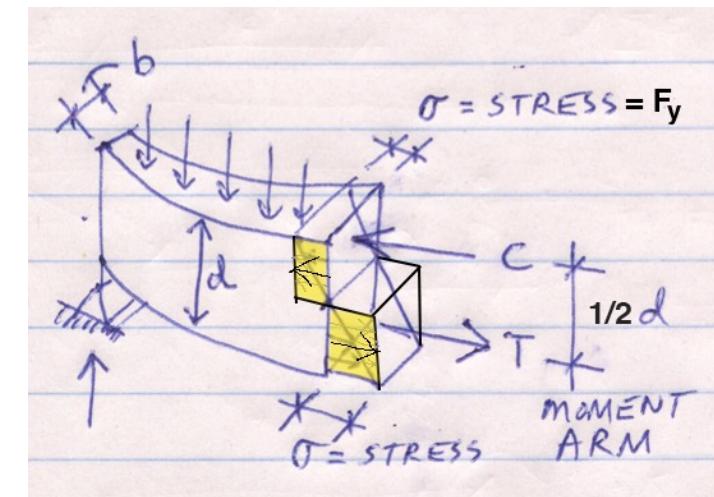
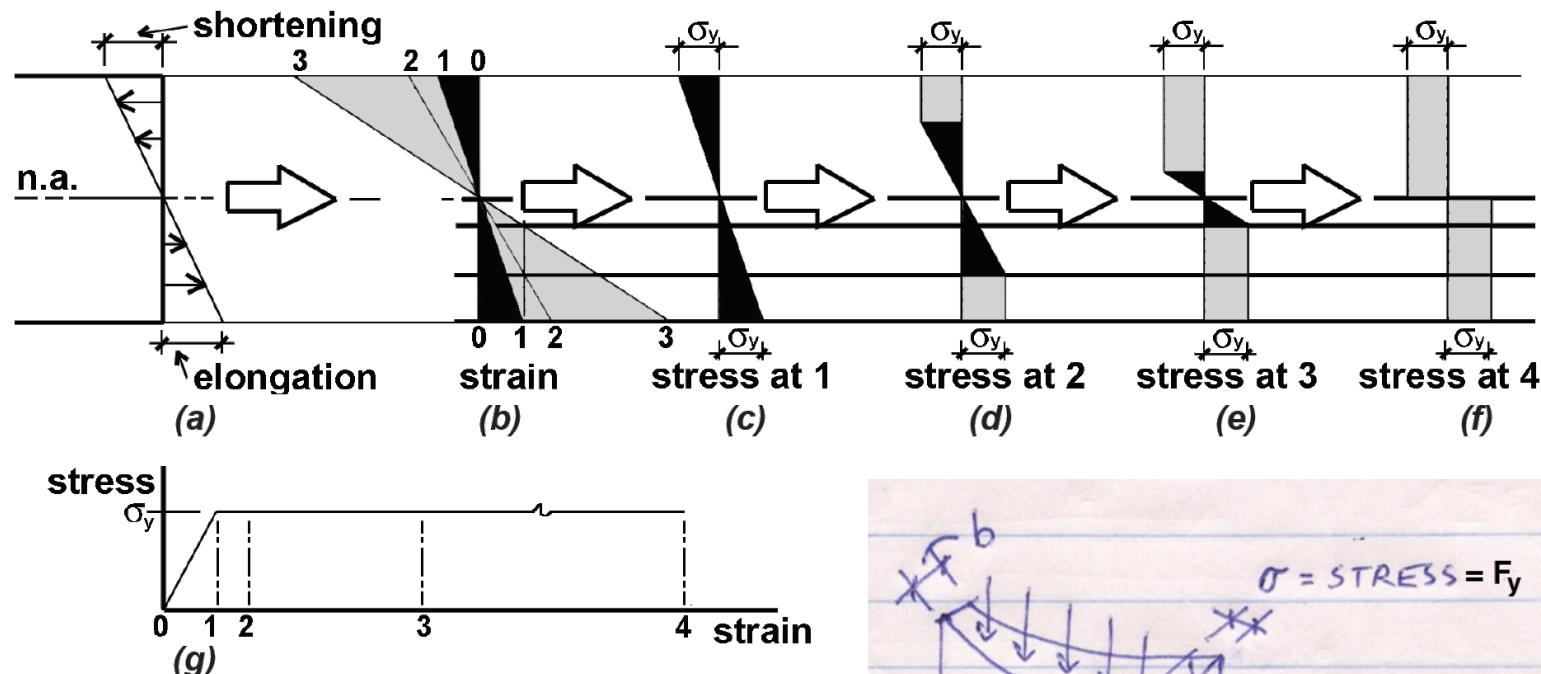


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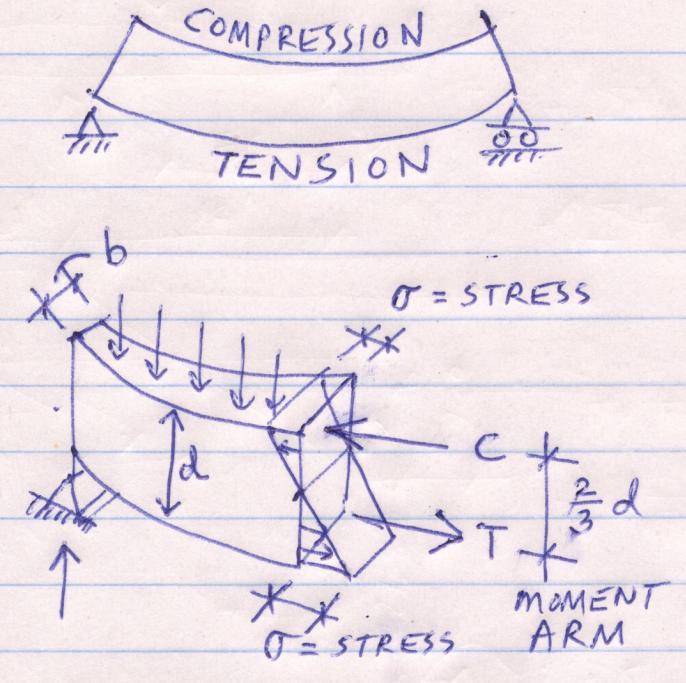
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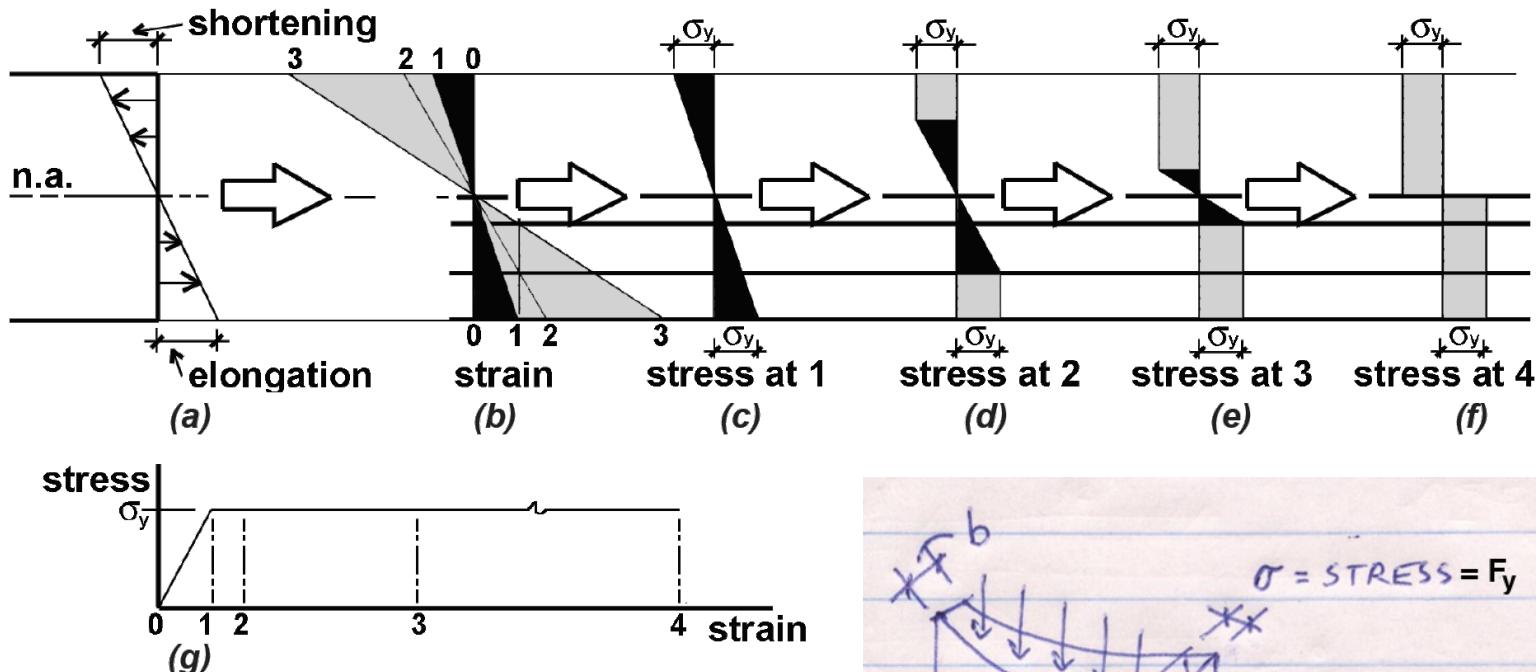


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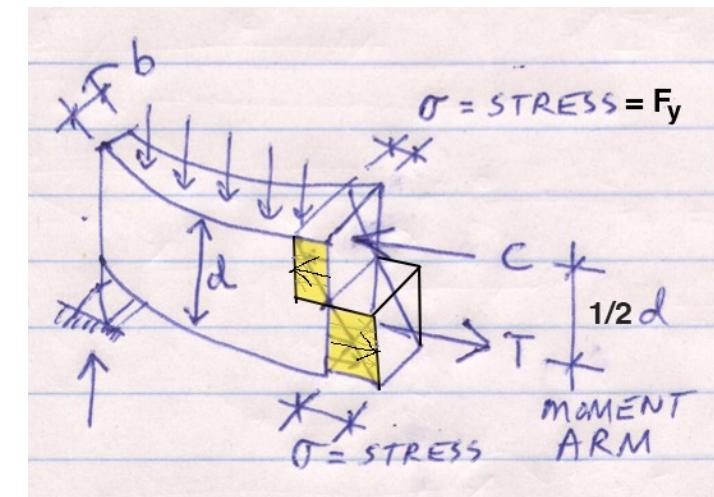
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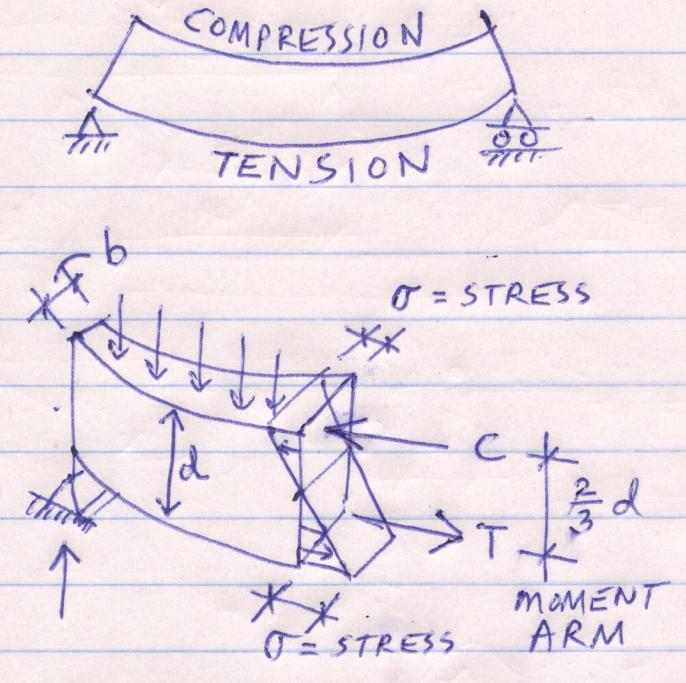
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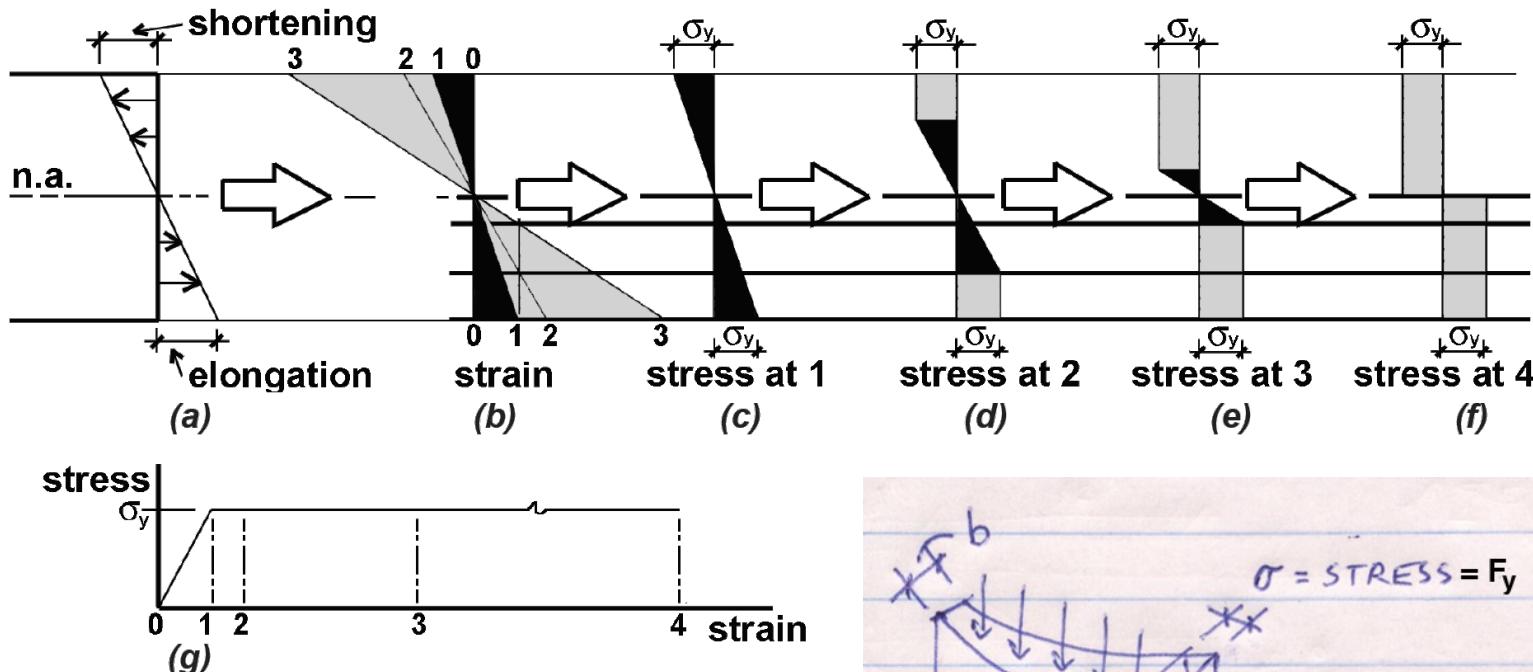


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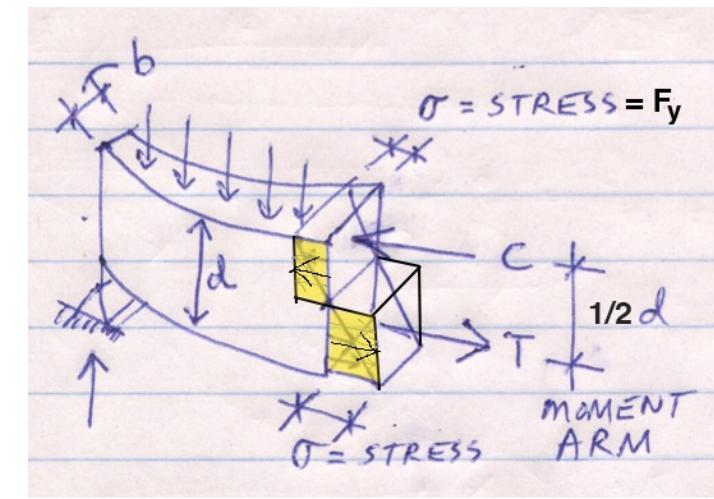
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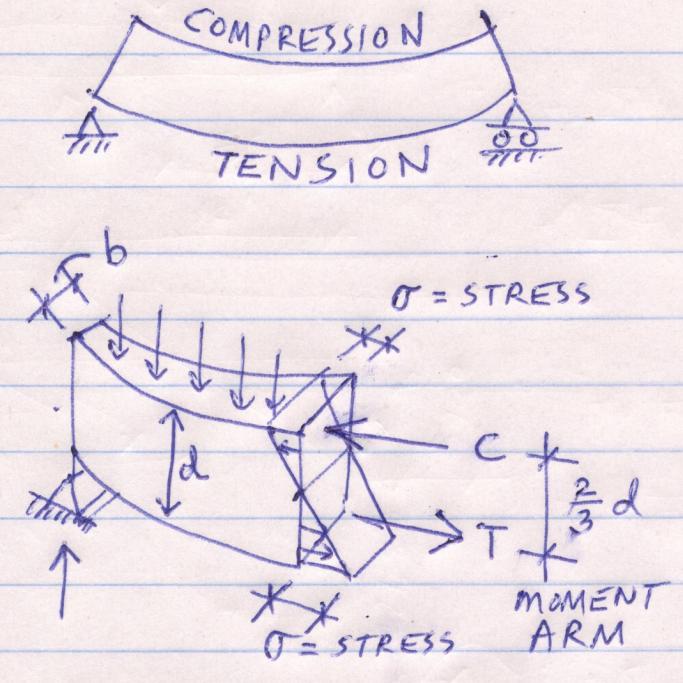


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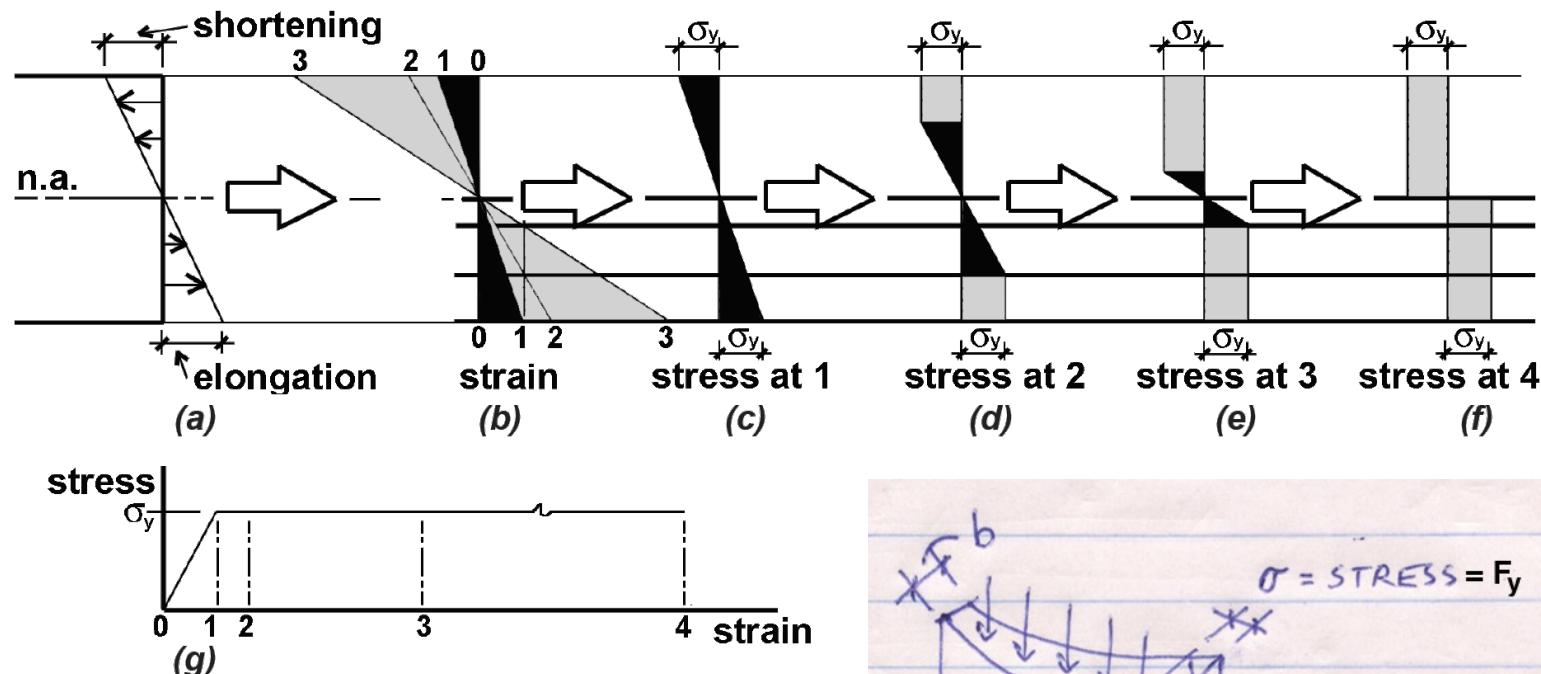
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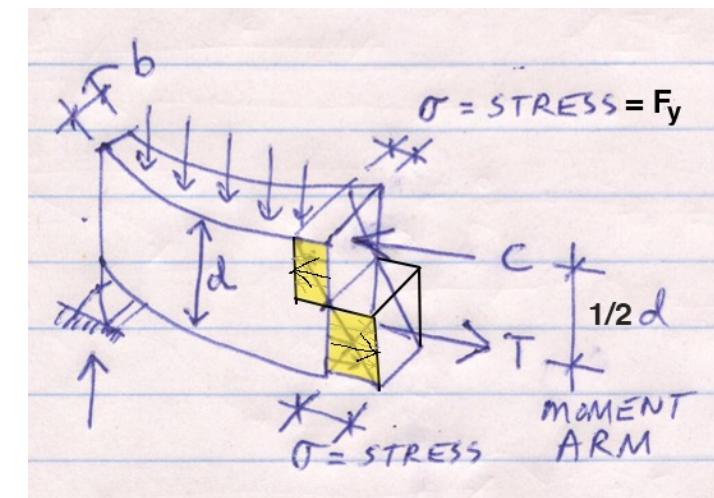
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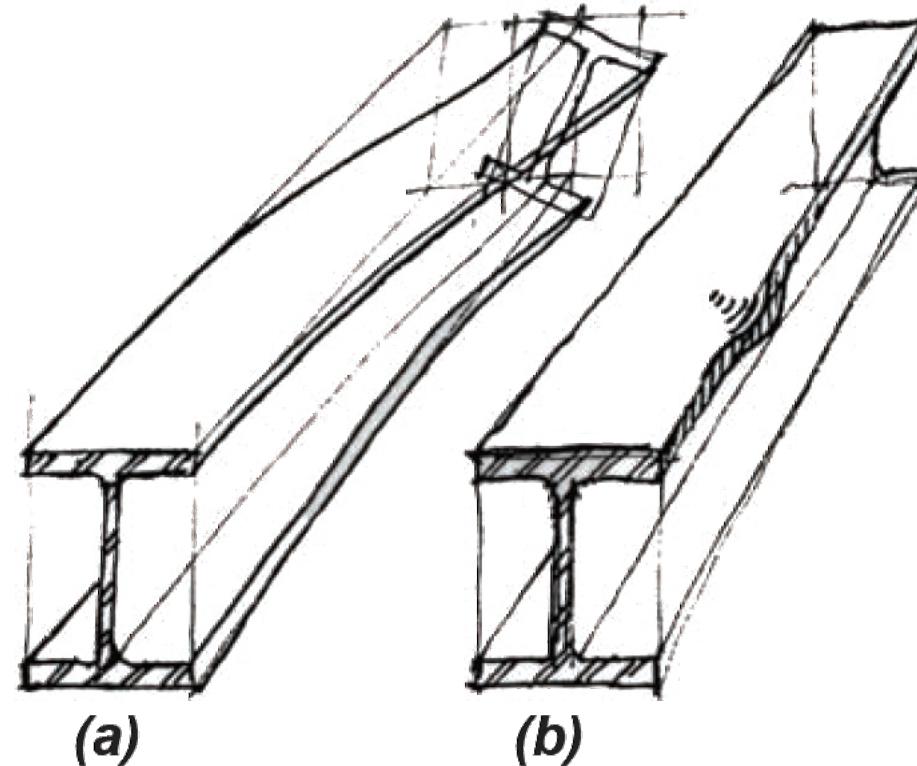
Substituting C into the first equation:
 $M = (F_y)(d/2)(b)(1/2)(d) = (F_y)(bd^2/4) = (F_y)(Z_x)$



Z_x is called the “plastic section modulus” and $Z_x = M / F_y$

Compact sections and the beam design equation

The equation for plastic section modulus, $Z_x = M/F_y$, presumes that the cross section is able to reach a state of complete yielding before one of two types of buckling occurs: either (a) lateral-torsional buckling within any unbraced segment along the length of the span or (b) local flange or web buckling.



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Therefore, to use this equation in design, based on the maximum moment encountered, the beam must be protected from both of these buckling modes, in the first case by limiting the effective length (typically happens “automatically” since the compressive flange is “braced” by the floor deck) and, in the second case, by regulating the proportions of the beam flange and web (i.e., using a so-called **compact section**).

Compact sections and the beam design equation

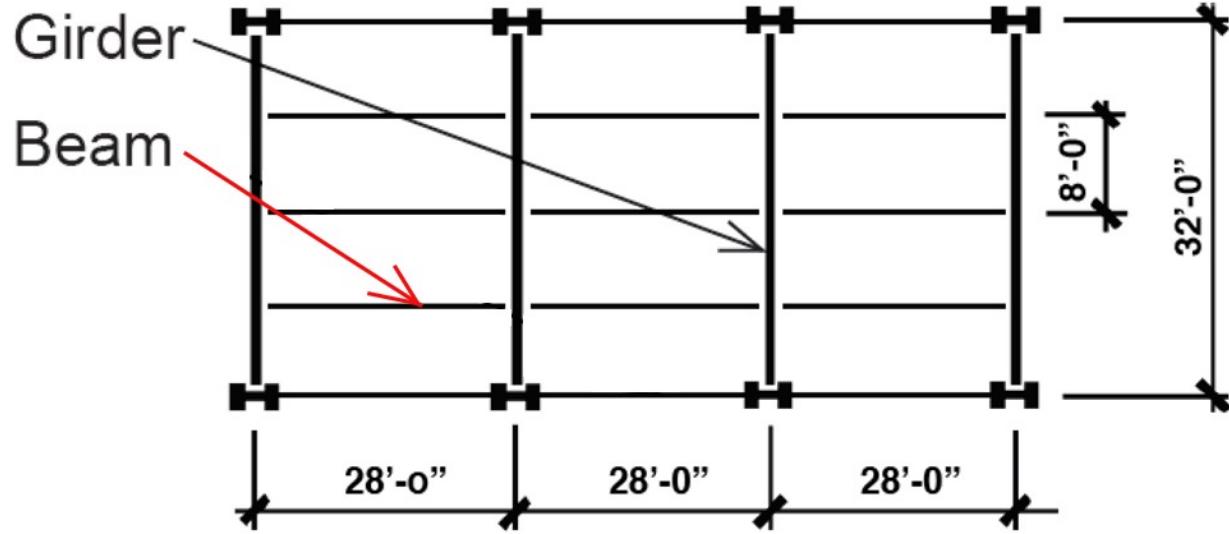
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Then, rewriting this equation in the form most useful for steel design, by adding a safety factor that limits the maximum stress in the beam to $0.6F_y$, we get:

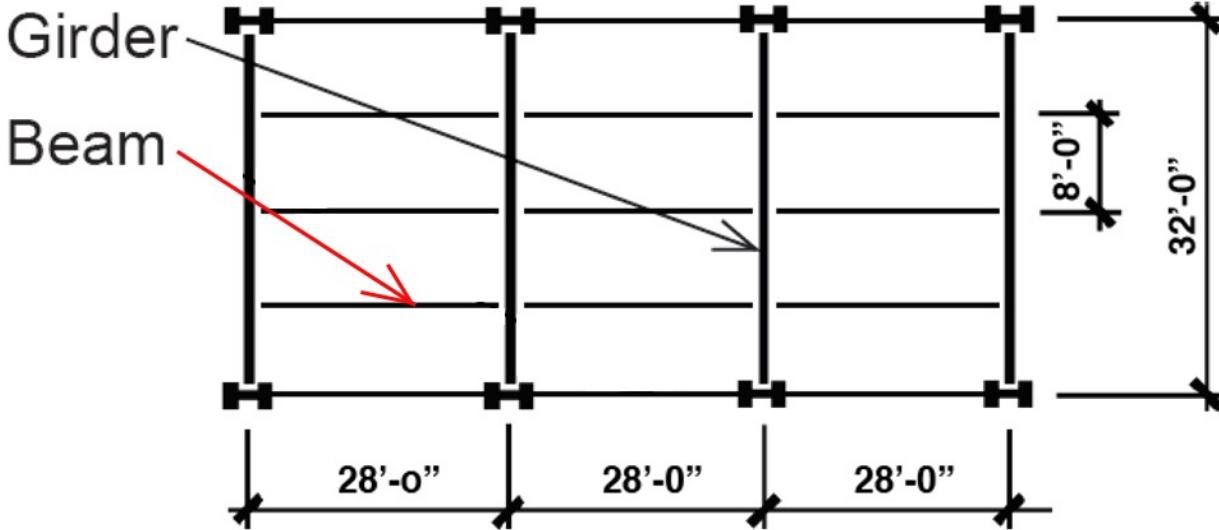
$$Z_{req} = M_{max} / (0.6F_y)$$

where M_{max} = the maximum bending moment (in-kips), F_y is the yield stress of the steel (ksi), and 0.6 is a safety factor for bending. The units of the required plastic section modulus are in³.



Framing plan

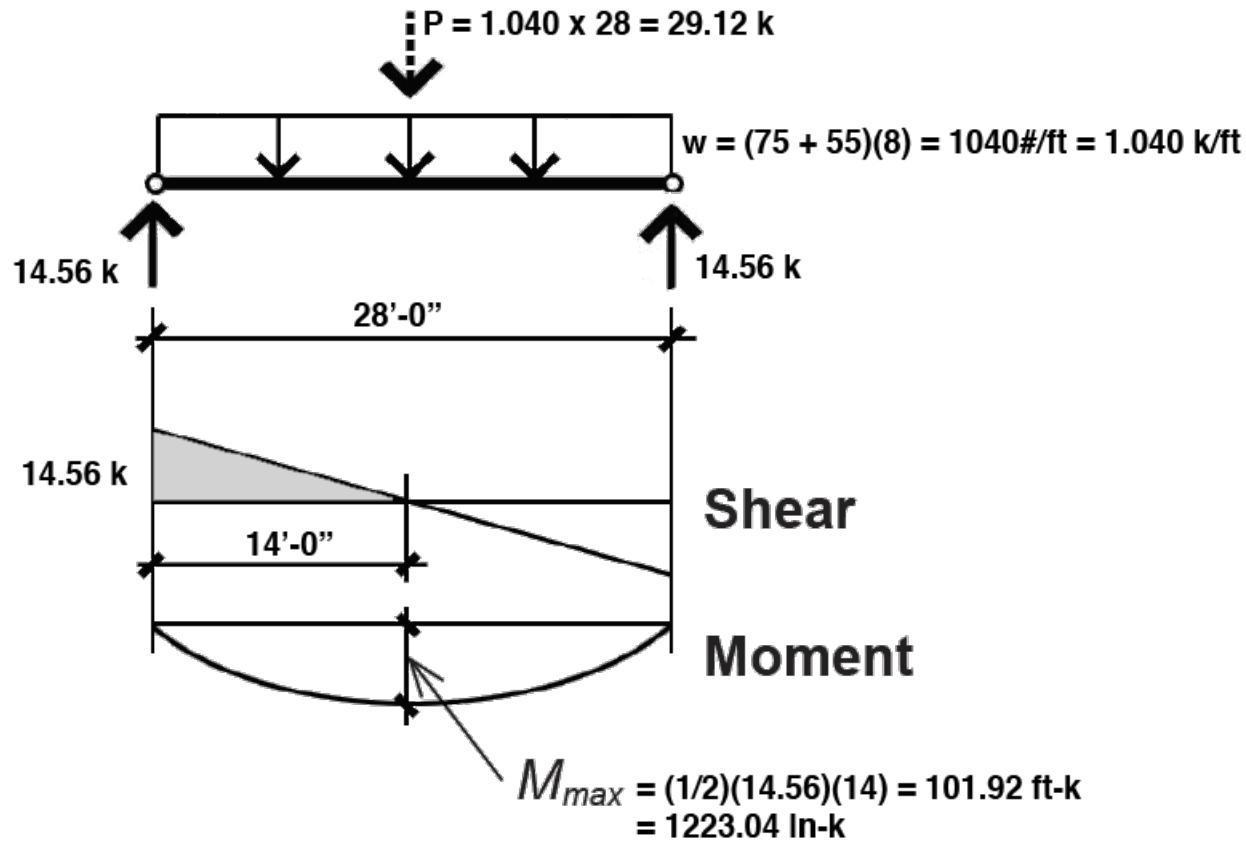
Design typical beam (no live load reduction).



Design typical beam (no live load reduction).

Assume L = 75 psf and D = 55 psf

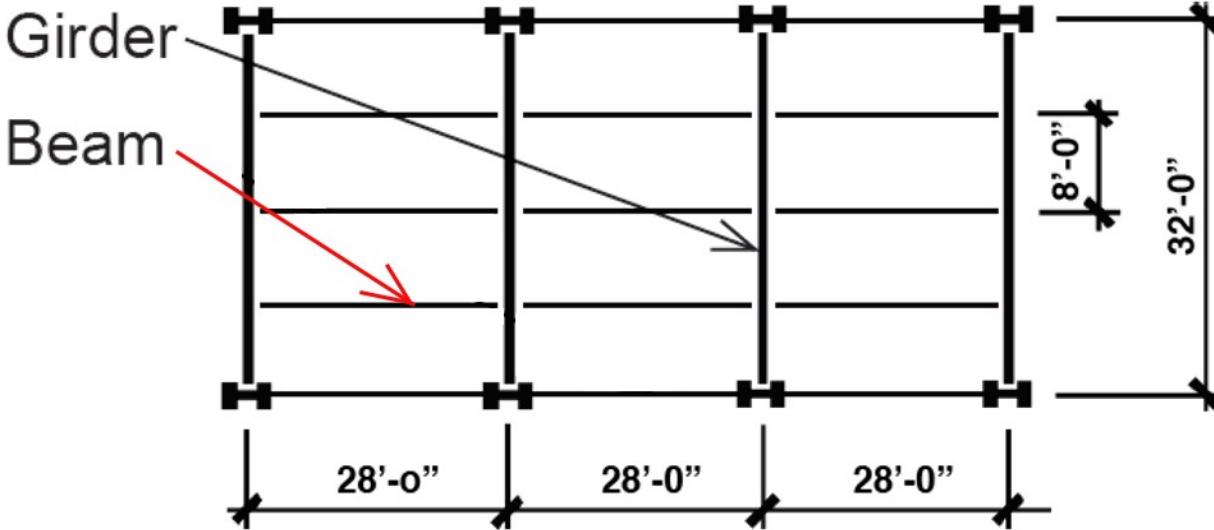
Use A-992 steel with $F_y = 50$ ksi



Chapter 4 — Steel: Appendix

Table A-4.1: Steel properties¹

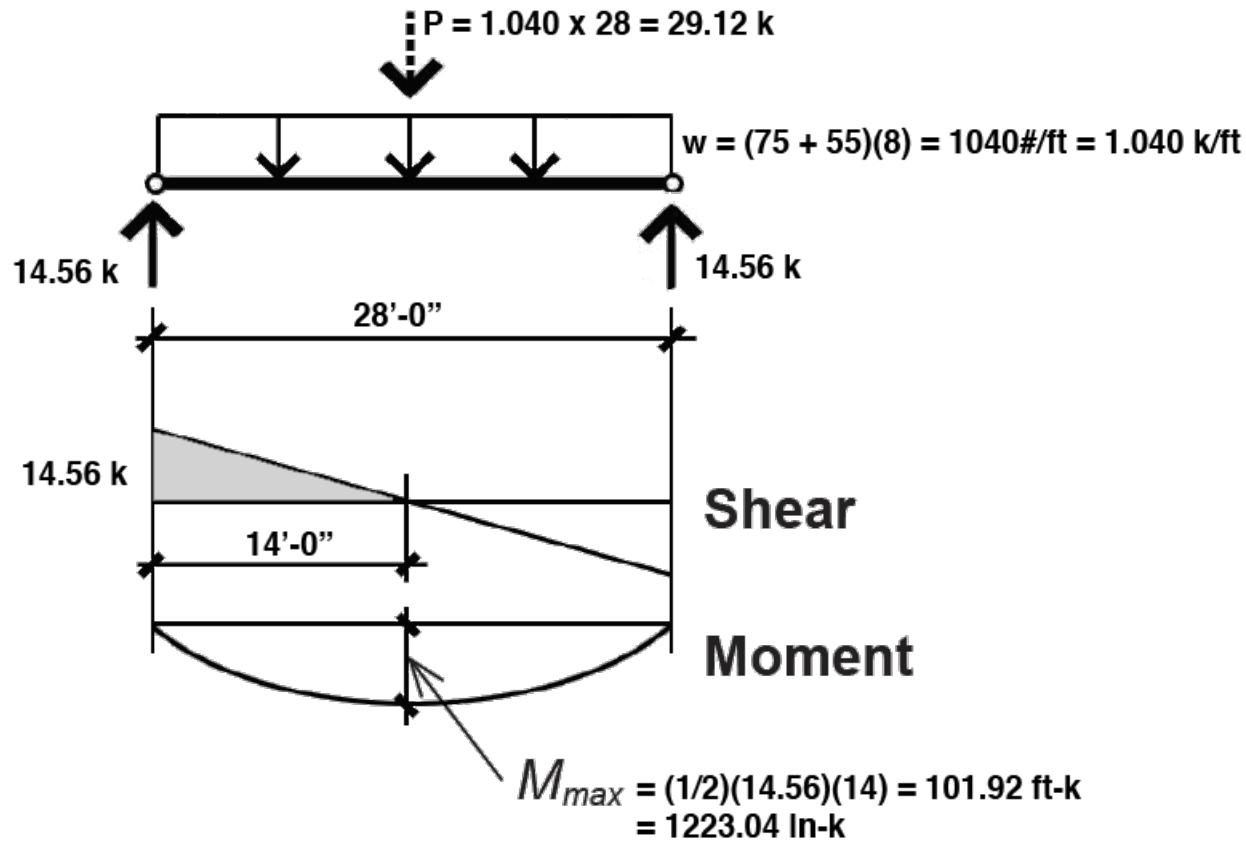
Category	ASTM designation	Yield stress, F_y (ksi)	(Ultimate) tensile stress, F_u (ksi)	Preferred for these shapes
Carbon	A36 A500 Gr. B A500 Gr. B A53 Gr. B	36 42 46 235	58 58 58 60	M, S, C, MC, L, plates ⁴ and bars HSS round ⁵ HSS rectangular ⁵ Pipe
High-strength, low-alloy	A992 A572 Gr. 50	50 50	65 65	³ W HP



Design typical beam (no live load reduction).

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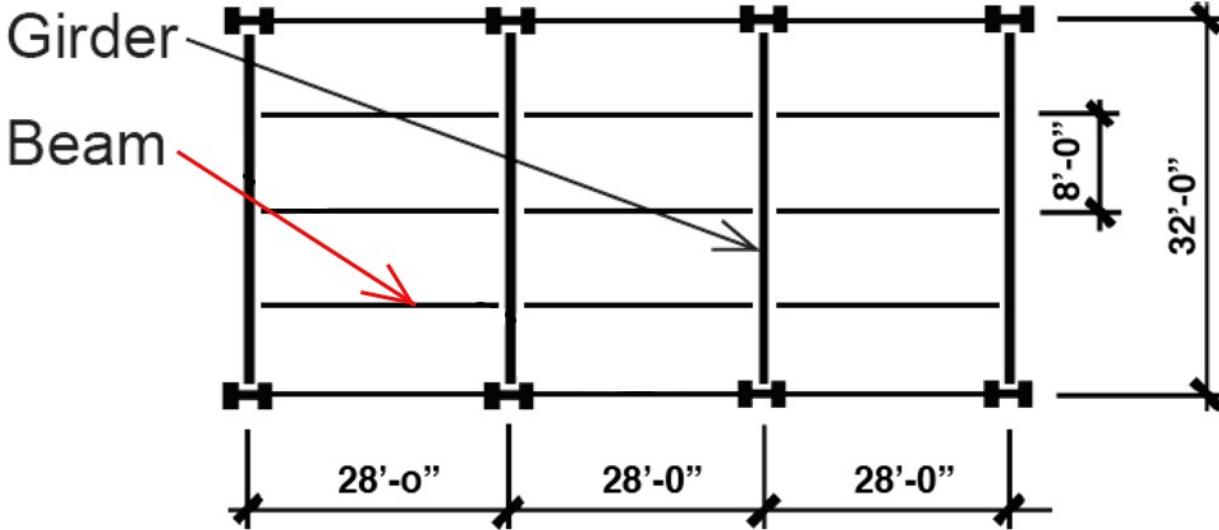


Chapter 4 — Steel: Appendix

$$Z_{req} = M_{max} / (0.6F_y)$$

Table A-4.1: Steel properties¹

Category	ASTM designation	Yield stress, F_y (ksi)	(Ultimate) tensile stress, F_u (ksi)	Preferred for these shapes
Carbon	A36	36	58	M, S, C, MC, L, plates ⁴ and bars
	A500 Gr. B	42	58	HSS round ⁵
	A500 Gr. B	46	58	HSS rectangular ⁵
	A53 Gr. B	35	60	Pipe
High-strength, low-alloy	A992	50	65	³ W
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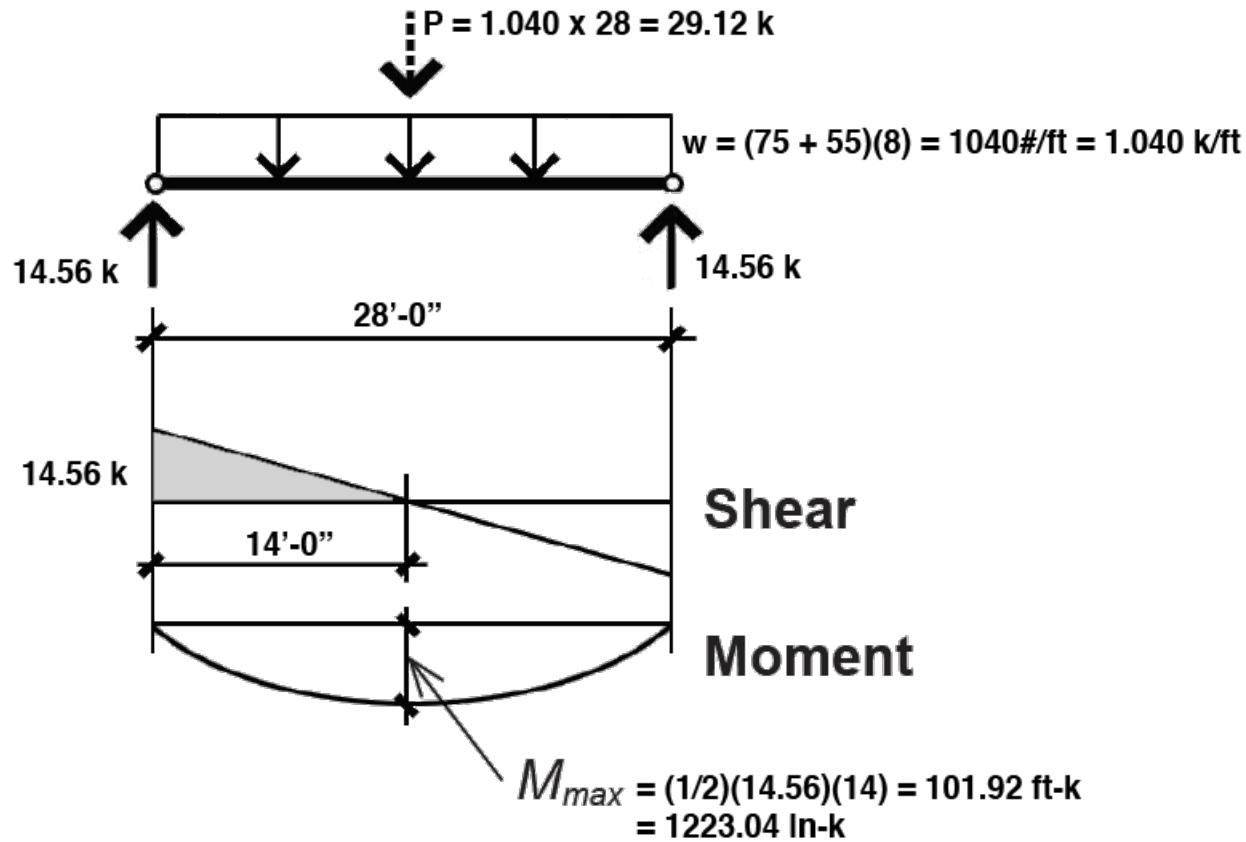


Framing plan

Design typical beam (no live load reduction).

Assume L = 75 psf and D = 55 psf

Use A-992 steel with $F_y = 50$ ksi



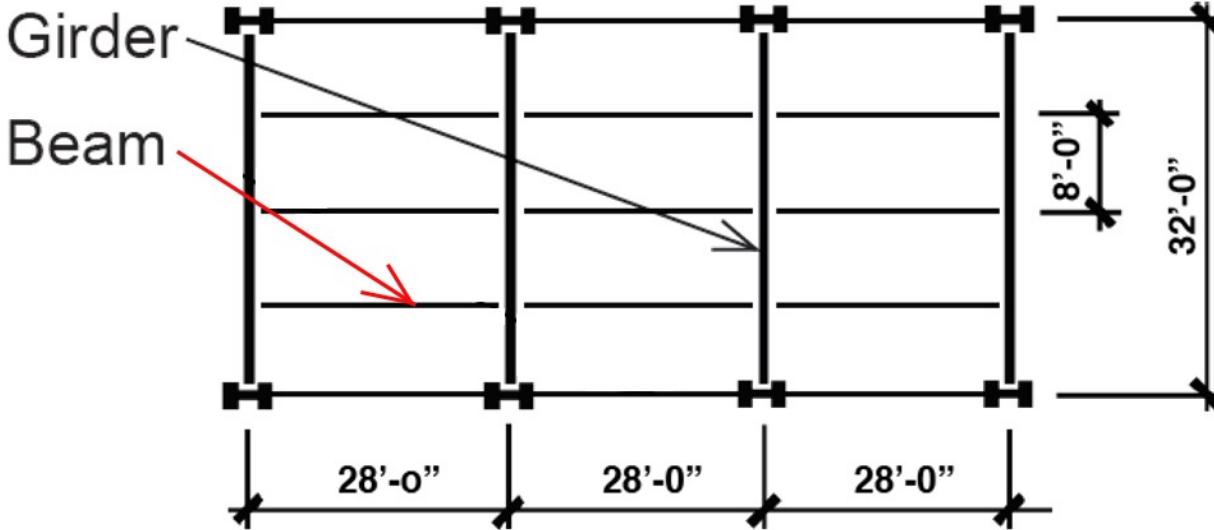
Chapter 4 — Steel: Appendix

$$Z_{req} = M_{max} / (0.6F_y)$$

$$Z_{req} = 1223.04 / (0.6 \times 50) = 40.77 \text{ in}^3$$

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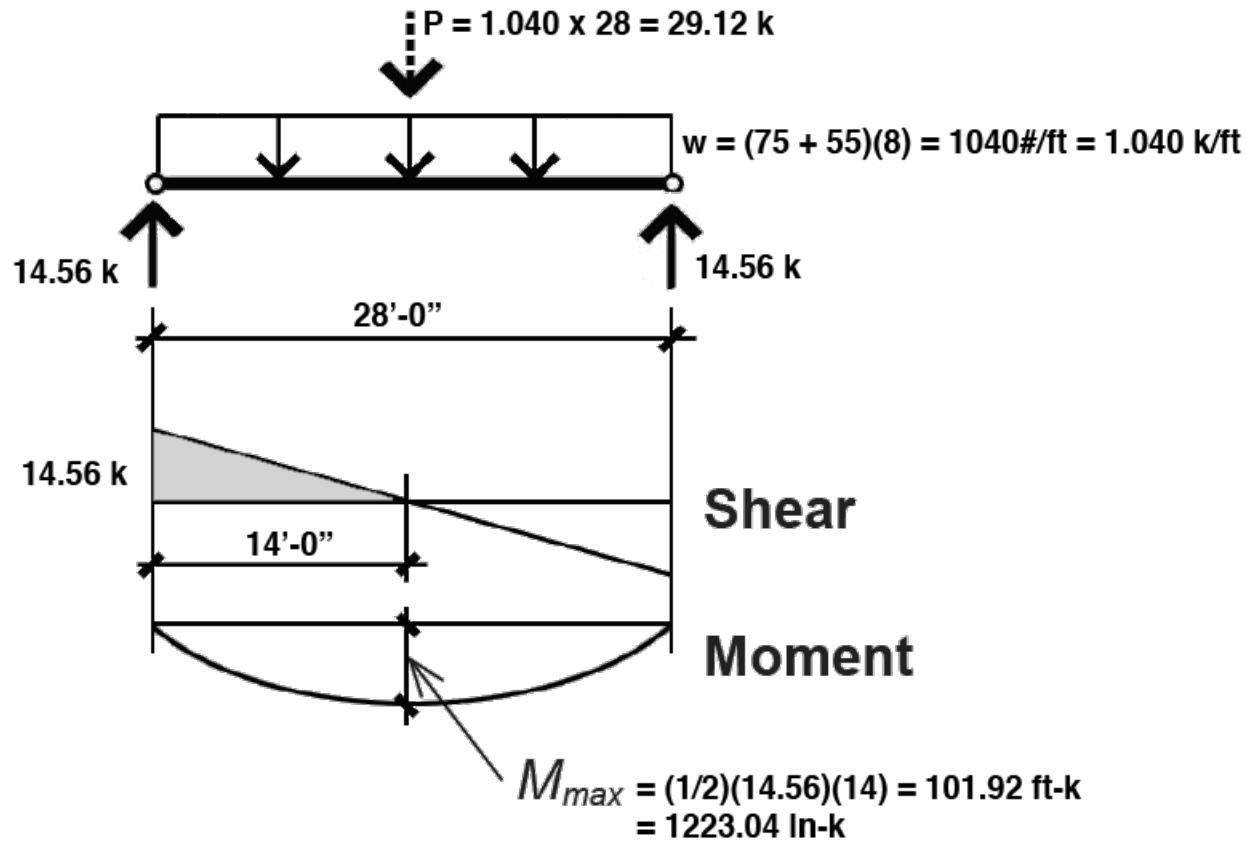
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High-strength, low-alloy	A992	50	65	³ W
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Design typical beam (no live load reduction).

Assume L = 75 psf and D = 55 psf

Use A-992 steel with $F_y = 50$ ksi



Chapter 4 — Steel: Appendix

$$Z_{req} = M_{max} / (0.6F_y)$$

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Select provisional section from Table A-4.15

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From Table A-4.15, select lightest section with a plastic section modulus of at least 40.77 in³

Table A-4.15: Plastic section modulus (Z_x) values: lightest laterally braced steel compact shapes for bending, $F_y = 50$ ksi

Shape	Z_x (in ³)	2L_p (ft)	Shape	Z_x (in ³)	2L_p (ft)	Shape	Z_x (in ³)	2L_p (ft)
W6 × 8.5 ¹	5.59	3.14	W21 × 55	126	6.11	W40 × 211	906	8.87
W6 × 9 ¹	6.23	3.20	W24 × 55	134	4.73	W40 × 215	964	12.5
W8 × 10 ¹	8.77	3.14	W21 × 62	144	6.25	W44 × 230	1100	12.1
W10 × 12 ¹	12.5	2.87	W24 × 62	153	4.87	W40 × 249	1120	12.5
W12 × 14	17.4	2.66	W21 × 68	160	6.36	W44 × 262	1270	12.3
W12 × 16	20.1	2.73	W24 × 68	177	6.61	W44 × 290	1410	12.3
W10 × 19	21.6	3.09	W24 × 76	200	6.78	W40 × 324	1460	12.6
W12 × 19	24.7	2.90	W24 × 84	224	6.89	W44 × 335	1620	12.3
W10 × 22	26.0	4.70	W27 × 84	244	7.31	W40 × 362	1640	12.7
W12 × 22	29.3	3.00	W30 × 90	283	7.38	W40 × 372	1680	12.7
W14 × 22	33.2	3.67	W30 × 99	312	7.42	W40 × 392	1710	9.33
W12 × 26	37.2	5.33	W30 × 108	346	7.59	W40 × 397	1800	12.9
W14 × 26	40.2	3.81	W30 × 116	378	7.74	W40 × 431	1960	12.9
W16 × 26	44.2	3.96	W33 × 118	415	8.19	W36 × 487	2130	14.0
W14 × 30	47.3	5.26	W33 × 130	467	8.44	W40 × 503	2320	13.1
W16 × 31	54.0	4.13	W36 × 135	509	8.41	W36 × 529	2330	14.1
W14 × 34	54.6	5.40	W33 × 141	514	8.58	W40 × 593	2760	13.4
W18 × 35	66.5	4.31	W40 × 149	598	8.09	W36 × 652	2910	14.5
W16 × 40	73.0	5.55	W36 × 160	624	8.83	W36 × 655	3080	13.6
W18 × 40	78.4	4.49	W40 × 167	693	8.48	W36 × 723	3270	14.7
W21 × 44	95.4	4.45	W36 × 182	718	9.01	W36 × 802	3660	14.9
W21 × 48	107	6.09	W40 × 183	774	8.80	W36 × 853	3920	15.1
W21 × 50	110	4.59	W40 × 199	869	12.2	W36 × 925	4130	15.0
W18 × 55	112	5.90						

From Table A-4.15, select lightest section with a plastic section modulus of at least 40.77 in³

Select a W16x26

Table A-4.15: Plastic section modulus (Z_x) values: lightest laterally braced steel compact shapes for bending, $F_y = 50$ ksi

Shape	Z_x (in ³)	2L_p (ft)	Shape	Z_x (in ³)	2L_p (ft)	Shape	Z_x (in ³)	2L_p (ft)
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Now, check for shear and deflection:

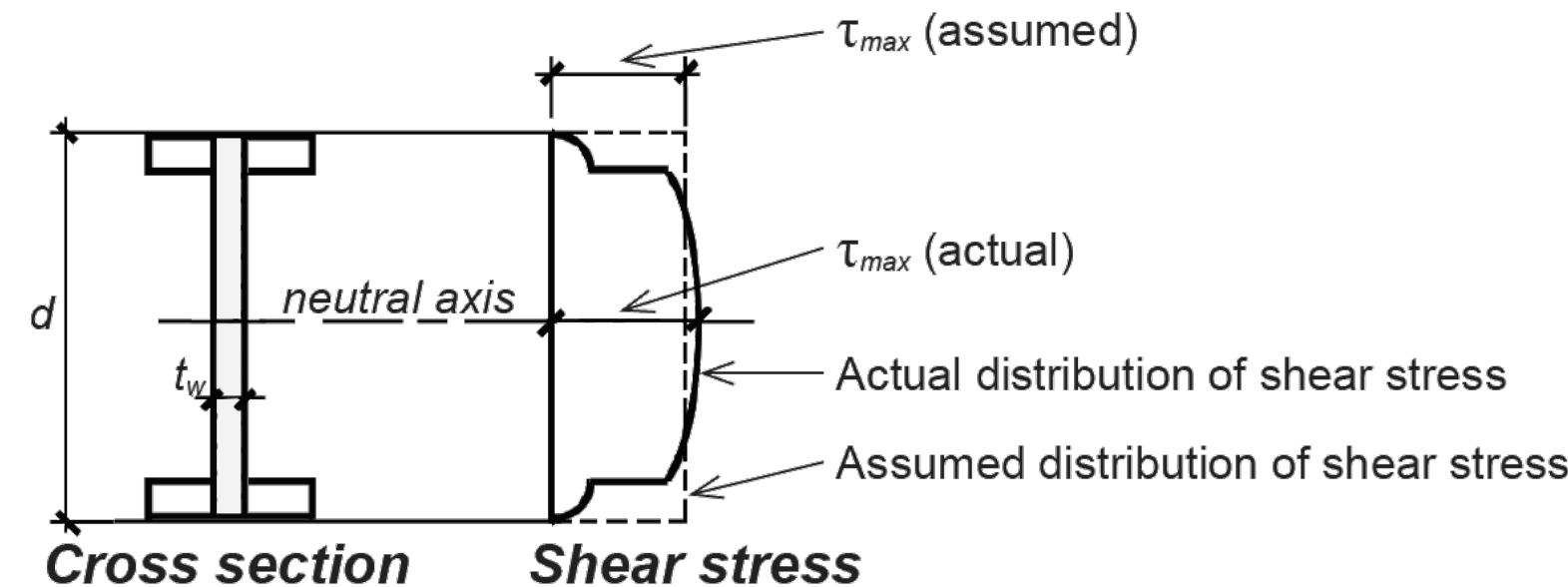
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W16 × 40	73.0	5.55	W36 × 160	624	8.83	W36 × 655	3080	13.6
W18 × 40	78.4	4.49	W40 × 167	693	8.48	W36 × 723	3270	14.7
W21 × 44	95.4	4.45	W36 × 182	718	9.01	W36 × 802	3660	14.9
W21 × 48	107	6.09	W40 × 183	774	8.80	W36 × 853	3920	15.1
W21 × 50	110	4.59	W40 × 199	869	12.2	W36 × 925	4130	15.0
W18 × 55	112	5.90						

For steel wide-flange shapes, simplified procedures have been developed, based on the **average** stress on the cross section, neglecting the overhanging flange areas; that is:

$$\tau_{max} = \frac{V}{dt_w} = V / A_w$$

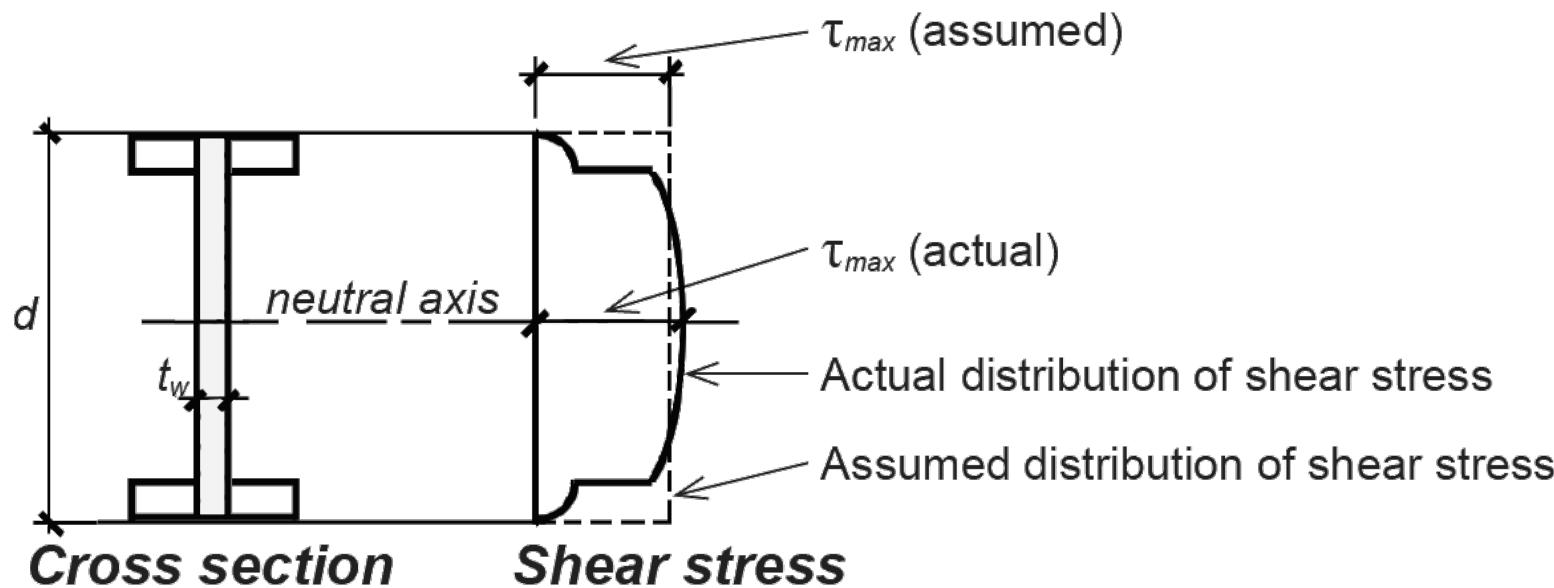
where τ_{max} = the maximum shear stress within the cross section, V = total shear force at the cross section, d = the cross-sectional depth, and t_w = the web thickness.



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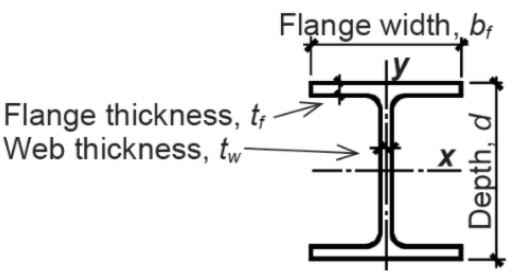


The “allowable” shear stress depends on the “slenderness” of the cross section (see Table A-4.3) and is set at $0.4F_y$ or $0.36F_y$ so that the equation for checking shear becomes:

Required web area, $A_w = V / (0.4F_y)$ or $A_w = V / (0.36F_y)$

We find section properties for the **W16x26** beam in Table A-4.3.

Table A-4.3: Dimensions and properties of steel W sections⁵



Cross-sectional area = A
 Moment of inertia = I
 Section modulus, $S_x = 2I_x/d$
 Sectional modulus, $S_y = 2I_y/b_f$
 Radius of gyration, $r_x = \sqrt{I_x/A}$
 Radius of gyration, $r_y = \sqrt{I_y/A}$

Designation	A (in 2)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in 3)	Z_x (in 3)	I_x (in 4)	I_y (in 4)	r_y (in.)
W14 × 426	125	18.7	1.88	16.7	3.04	706	869	6600	2360	4.34
W14 × 455	134	19.0	2.02	16.8	3.21	756	936	7190	2560	4.38
W14 × 500	147	19.6	2.19	17.0	3.50	838	1050	8210	2880	4.43
W14 × 550	162	20.2	2.38	17.2	3.82	931	1180	9430	3250	4.49
W14 × 605	178	20.9	2.60	17.4	4.16	1040	1320	10800	3680	4.55
W14 × 665	196	21.6	2.83	17.7	4.52	1150	1480	12400	4170	4.62
W14 × 730	215	22.4	3.07	17.9	4.91	1280	1660	14300	4720	4.69
W14 × 808	238	22.8	3.74	18.6	5.12	1390	1830	15900	5550	4.83
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W16 × 26 ^{3,4}	7.68	15.7	0.250	5.50	0.345	38.4	44.2	301	9.59	1.12
W16 × 31 ⁴	9.13	15.9	0.275	5.53	0.440	47.2	54.0	375	12.4	1.17
W16 × 36 ⁴	10.6	15.9	0.295	6.99	0.430	56.5	64.0	448	24.5	1.52
W16 × 40 ⁴	11.8	16.0	0.305	7.00	0.505	64.7	73.0	518	28.9	1.57
W16 × 45 ⁴	13.3	16.1	0.345	7.04	0.565	72.7	82.3	586	32.8	1.57
W16 × 50 ⁴	14.7	16.3	0.380	7.07	0.630	81.0	92.0	659	37.2	1.59
W16 × 57	16.8	16.4	0.430	7.12	0.715	92.2	105	758	43.1	1.60

Notes:

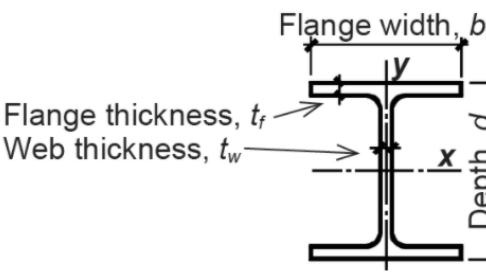
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3. Section webs do not meet slenderness criteria for shear for which the allowable stress can be taken as $F_v = 0.4F_y$; instead, use a reduced allowable shear stress, $F_v = 0.36F_y$.
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We find section properties for the **W16x26** beam in Table A-4.3.

This is also where we find out whether to use a safety factor of 0.4 or **0.36**.

From footnote 3 marked next to the section, we use a safety factor of **3.6**.

Table A-4.3: Dimensions and properties of steel W sections⁵



Cross-sectional area = A
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 Radius of gyration, $r_x = \sqrt{I_x/A}$
 Radius of gyration, $r_y = \sqrt{I_y/A}$

Designa-tion	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W14 × 426	125	18.7	1.88	16.7	3.04	706	869	6600	2360	4.34
W14 × 455	134	19.0	2.02	16.8	3.21	756	936	7190	2560	4.38
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Notes:

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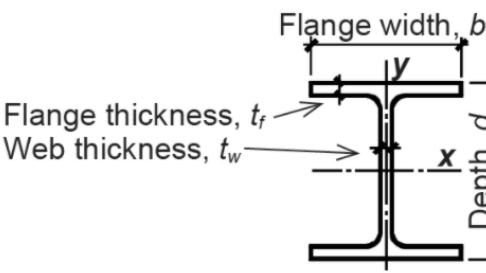
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Since $V = 14.56 \text{ k}$ and $F_y = 50 \text{ ksi}$, the required web area, $A_w = 14.56 / (0.36 \times 50) = 0.809 \text{ in}^2$

Table A-4.3: Dimensions and properties of steel W sections⁵



Cross-sectional area = A
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 Section modulus, $S_x = 2I_x/d$
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Designa-tion	A (in 2)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in 3)	Z_x (in 3)	I_x (in 4)	I_y (in 4)	r_y (in.)
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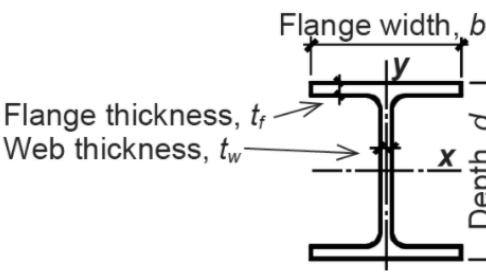
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We compare this required web area to the actual web area by finding d and t_w in **Table A-4.3.**

Table A-4.3: Dimensions and properties of steel W sections⁵



Designation	A (in 2)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in 3)	Z_x (in 3)	I_x (in 4)	I_y (in 4)	r_y (in.)
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W16 × 26 ^{3,4}	7.68	15.7	0.250	5.50	0.345	38.4	44.2	301	9.59	1.12
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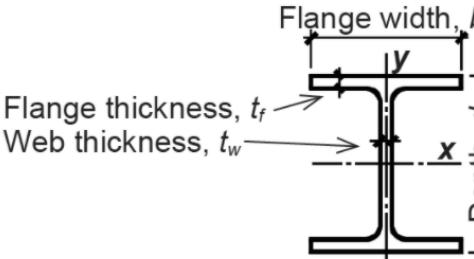
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Since $V = 14.56 \text{ k}$ and $F_y = 50 \text{ ksi}$, the required web area, $A_w = 14.56 / (0.36 \times 50) = 0.809 \text{ in}^2$

We compare this required web area to the actual web area by finding d and t_w in Table A-4.3.

$d = 15.7 \text{ in.}$ and $t_w = 0.25 \text{ in.}$ Therefore, the actual web area = $15.7 \times 0.25 = 3.925 \text{ in}^2$.

Table A-4.3: Dimensions and properties of steel W sections⁵



Designation	A (in 2)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in 3)	Z_x (in 3)	I_x (in 4)	I_y (in 4)	r_y (in.)
W14 x 426	125	18.7	1.88	16.7	3.04	706	869	6600	2360	4.34
W14 x 455	134	19.0	2.02	16.8	3.21	756	936	7190	2560	4.38
W14 x 500	147	19.6	2.19	17.0	3.50	838	1050	8210	2880	4.43
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W14 x 873	257	23.6	3.94	18.8	5.51	1530	2030	18100	6170	4.90
W16 x 26 ^{3,4}	7.68	15.7	0.250	5.50	0.345	38.4	44.2	301	9.59	1.12
W16 x 31 ⁴	9.13	15.9	0.275	5.53	0.440	47.2	54.0	375	12.4	1.17
W16 x 36 ⁴	10.6	15.9	0.295	6.99	0.430	56.5	64.0	448	24.5	1.52
W16 x 40 ⁴	11.8	16.0	0.305	7.00	0.505	64.7	73.0	518	28.9	1.57
W16 x 45 ⁴	13.3	16.1	0.345	7.04	0.565	72.7	82.3	586	32.8	1.57
W16 x 50 ⁴	14.7	16.3	0.380	7.07	0.630	81.0	92.0	659	37.2	1.59
W16 x 57	16.8	16.4	0.430	7.12	0.715	92.2	105	758	43.1	1.60

Notes:

1. Section not compact for steel with $F_y = 36 \text{ ksi}$ or $F_y = 50 \text{ ksi}$.
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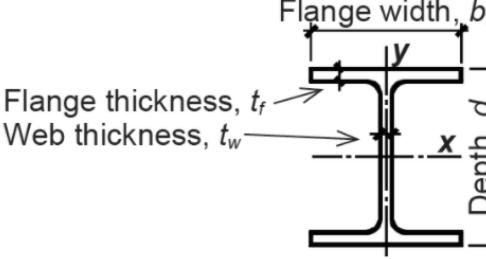
Since $V = 14.56 \text{ k}$ and $F_y = 50 \text{ ksi}$, the required web area, $A_w = 14.56 / (0.36 \times 50) = 0.809 \text{ in}^2$

We compare this required web area to the actual web area by finding d and t_w in Table A-4.3.

$d = 15.7 \text{ in.}$ and $t_w = 0.25 \text{ in.}$ Therefore, the actual web area = $15.7 \times 0.25 = 3.925 \text{ in}^2$.

Since the actual web area is greater or equal to the required web area, **the section is OK for shear.**

Table A-4.3: Dimensions and properties of steel W sections⁵

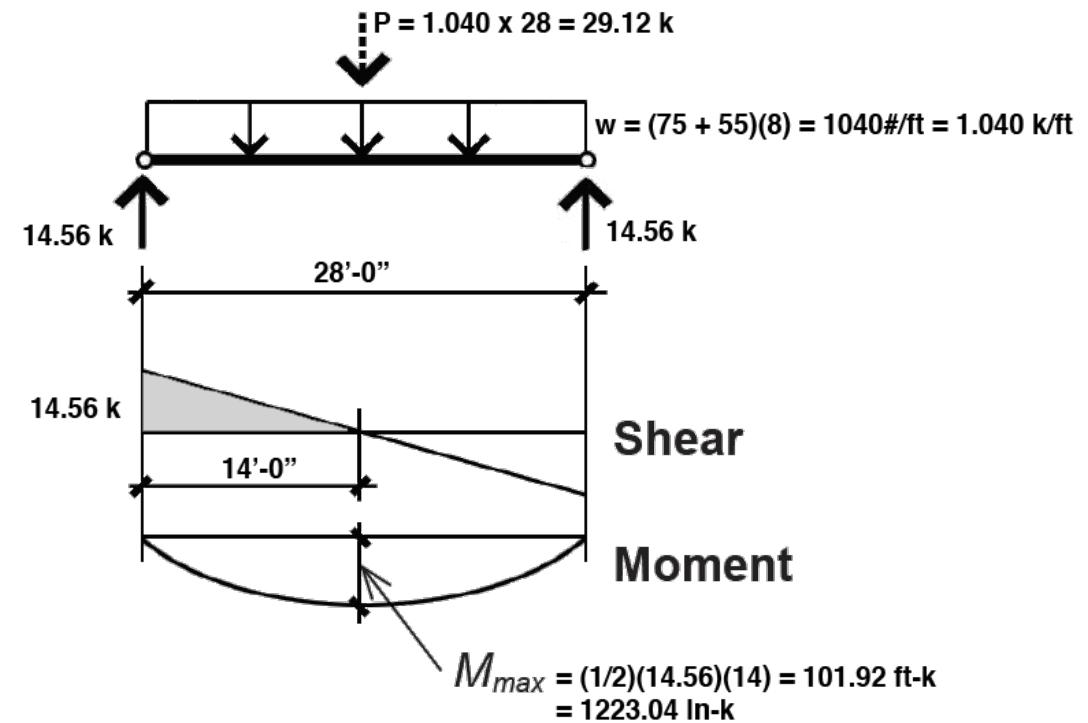


Designation	A (in 2)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in 3)	Z_x (in 3)	I_x (in 4)	I_y (in 4)	r_y (in.)
W14 × 426	125	18.7	1.88	16.7	3.04	706	869	6600	2360	4.34
W14 × 455	134	19.0	2.02	16.8	3.21	756	936	7190	2560	4.38
W14 × 500	147	19.6	2.19	17.0	3.50	838	1050	8210	2880	4.43
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W16 × 26 ^{3,4}	7.68	15.7	0.250	5.50	0.345	38.4	44.2	301	9.59	1.12
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W16 × 50 ⁴	14.7	16.3	0.380	7.07	0.630	81.0	92.0	659	37.2	1.59
W16 × 57	16.8	16.4	0.430	7.12	0.715	92.2	105	758	43.1	1.60

Notes:

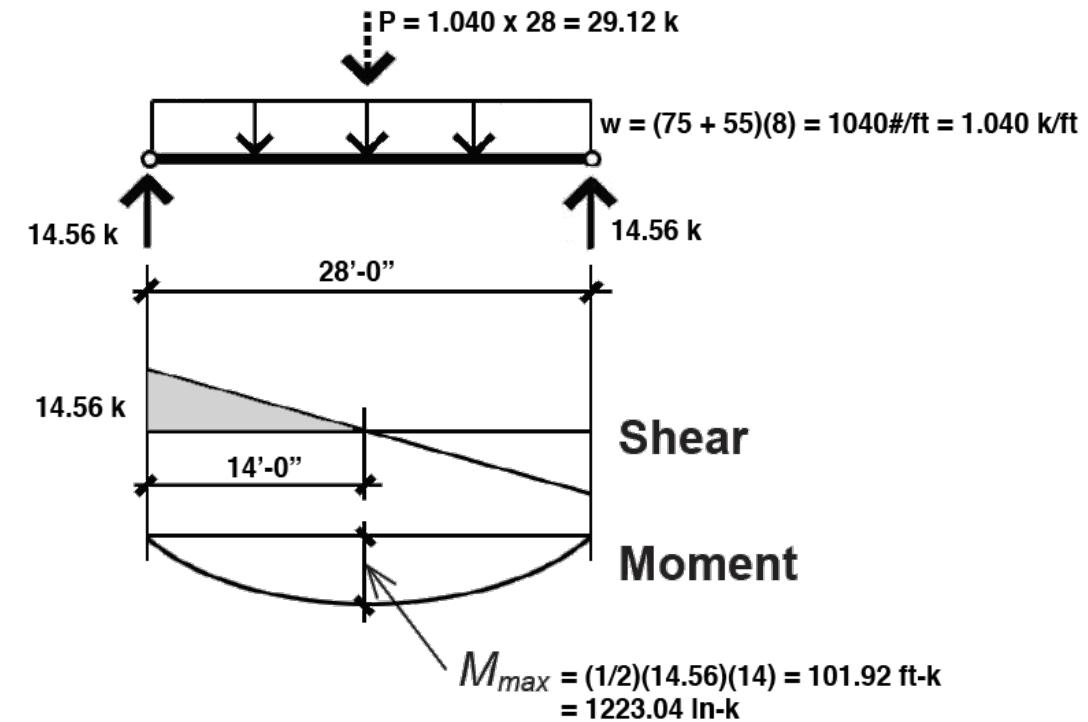
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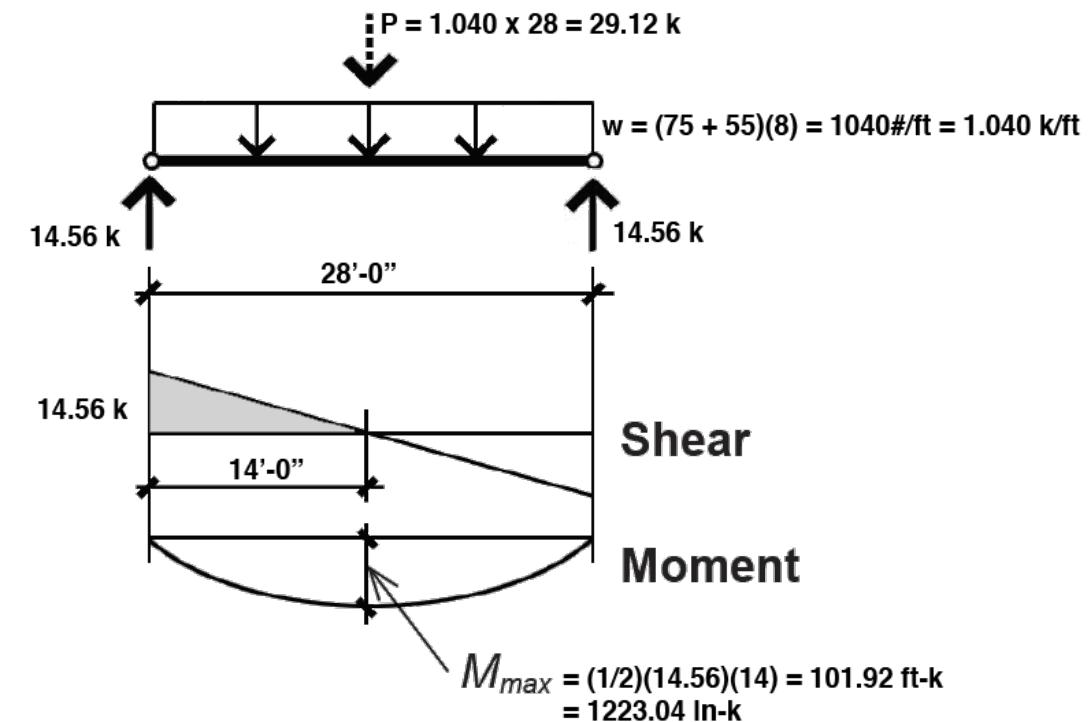
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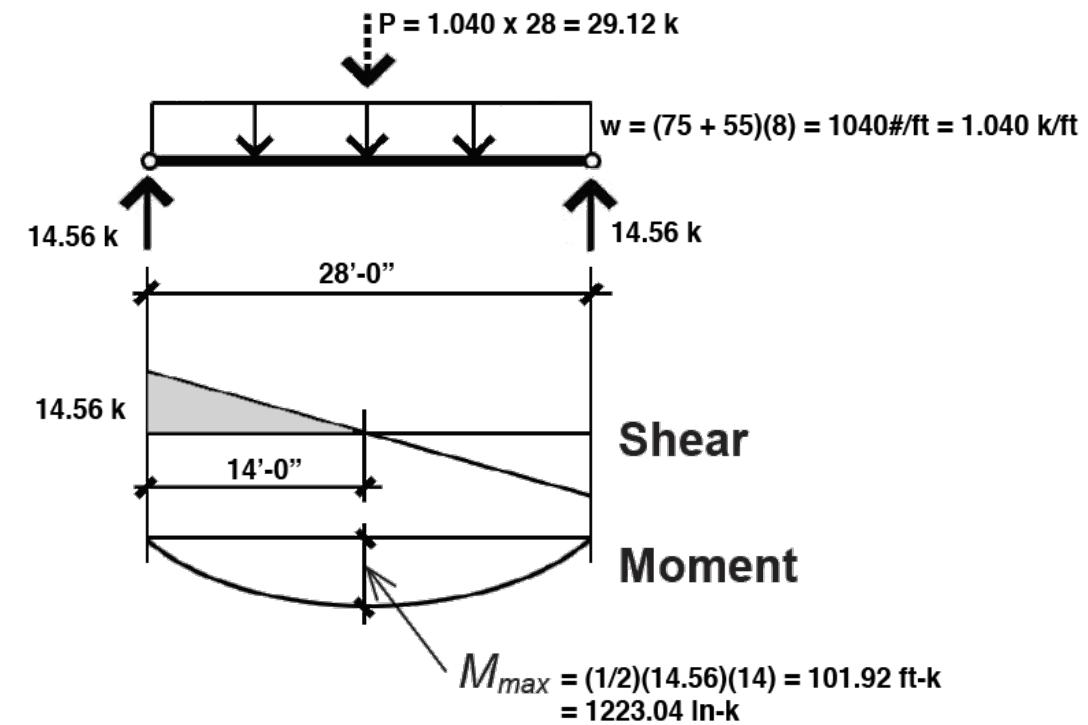
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Table A-3.15: Maximum (actual) deflection in a beam^{1,2,3}

Deflection coefficient, C , for maximum (actual) deflection, Δ (in.), where $\Delta = \frac{CP(L/12)^3}{EI_x}$				
$P = w(L/12)$ 	22.46	9.33	4.49	216
	35.94	16.07	8.99	n/a
	61.34	26.27	13.31	n/a
	85.54	36.12	17.97	n/a
	n/a	n/a	n/a	576



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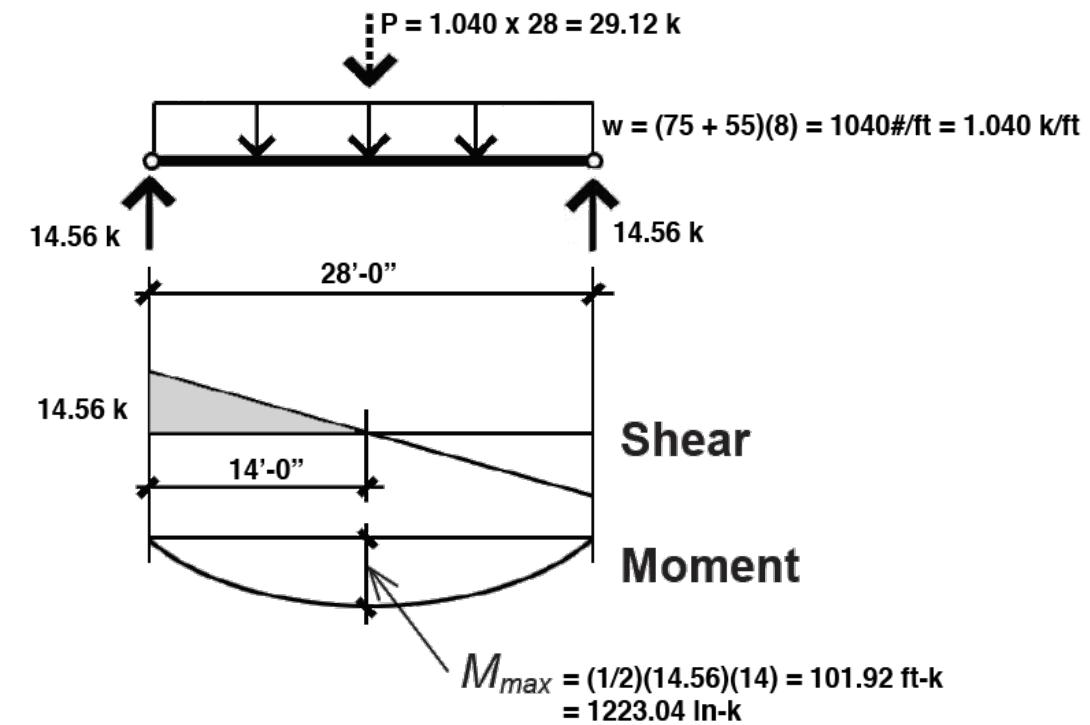
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The other parameters are easily determined:

$P = w(L/12)$ where w is either the live load or the total load (#/ft) and L is the span in inches (so $L/12$ is the span in feet).

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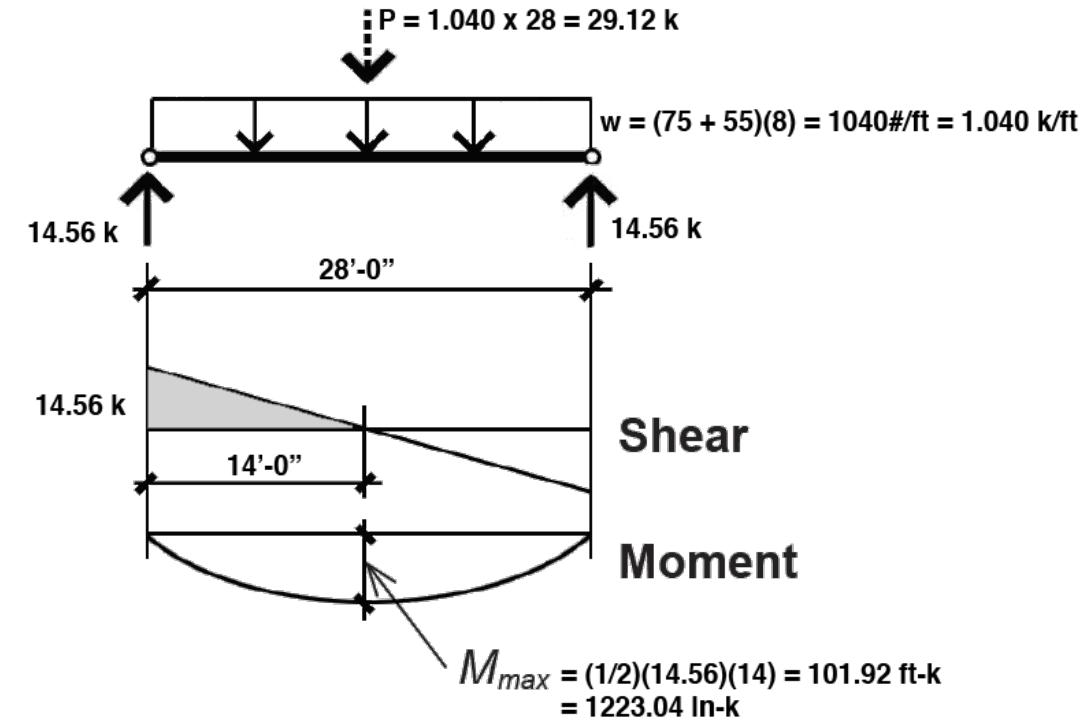
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Now, it turns out that we need to check the maximum deflection under two load scenarios: total load and live load. Why??

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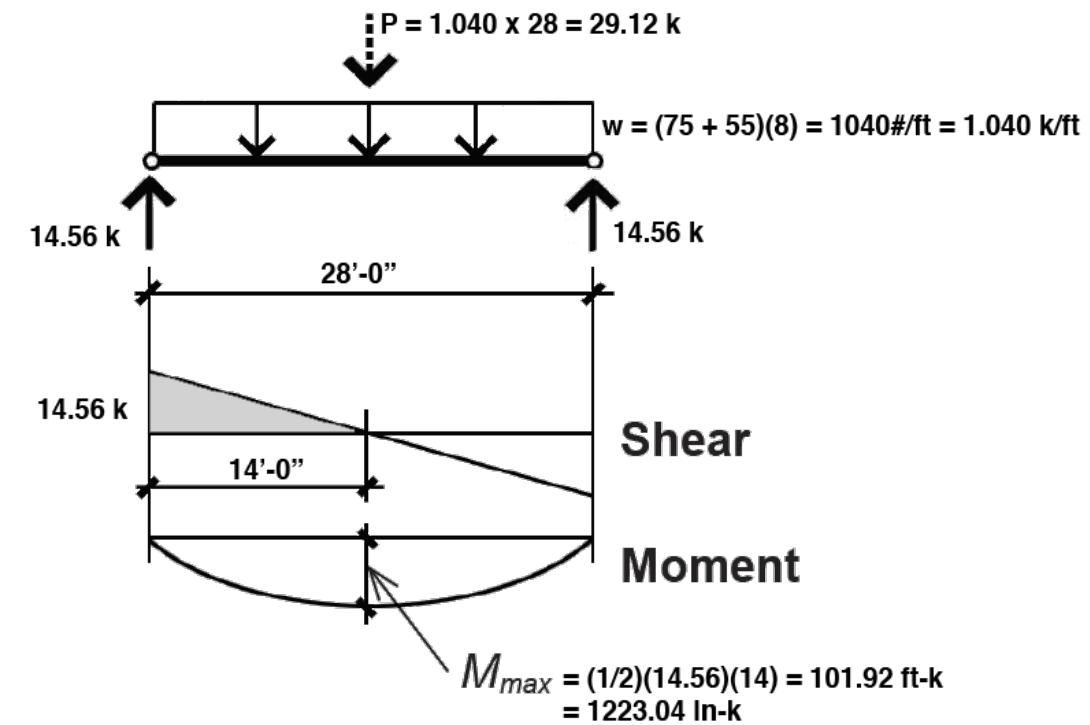
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Because live load by itself might crack a “plaster” ceiling; while total load deflection might be unsightly, or correspond to vibration or bounciness in the floor.

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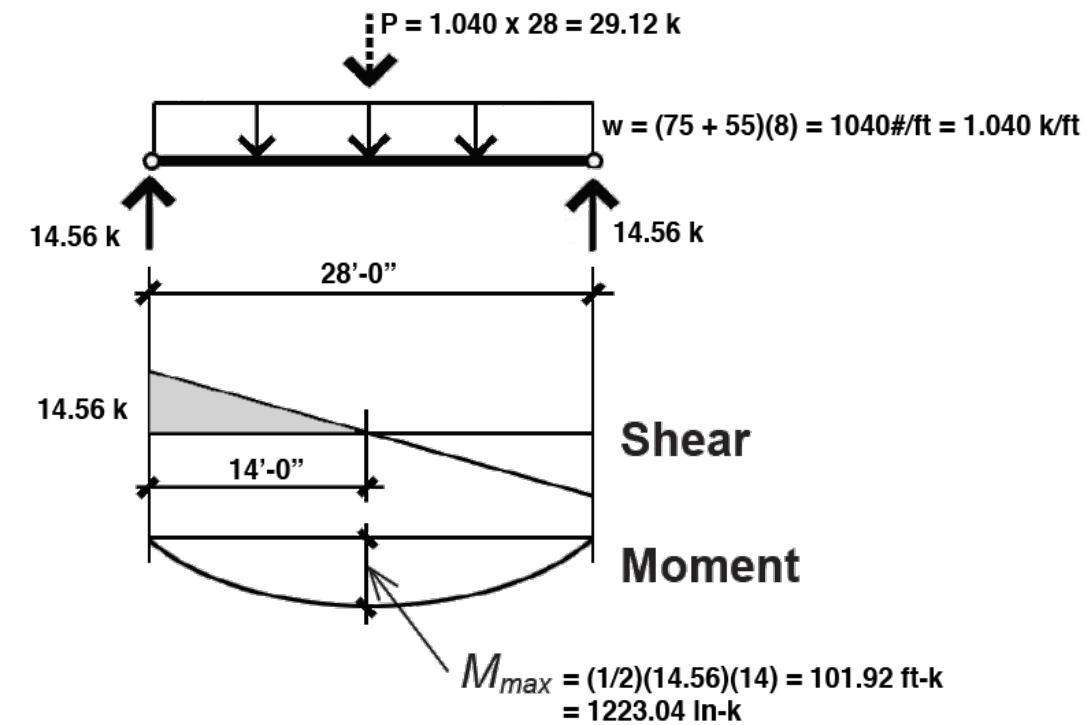
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Now, it turns out that we need to check the maximum deflection under two load scenarios: total load and live load. Why??

Because live load by itself might crack a “plaster” ceiling; while total load deflection might be unsightly, or correspond to vibration or bounciness in the floor.

Start with total load deflection.

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TOTAL LOAD DEFLECTION:

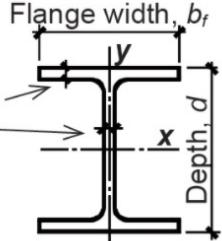
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High-strength, low-alloy	A992 A572 Gr. 50	50 50	65 65	³ W HP

Notes:

1. The modulus of elasticity, E , for these steels can be taken as 29,000 ksi.

Table A-4.3: Dimensions and properties of steel W sections⁵



Cross-sectional area = A
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Designation	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W14 × 730	215	22.4	3.07	17.9	4.91	1280	1660	14300	4720	4.69
W14 × 808	238	22.8	3.74	18.6	5.12	1390	1830	15900	5550	4.83
W14 × 873	257	23.6	3.94	18.8	5.51	1530	2030	18100	6170	4.90
W16 × 26 ^{3,4}	7.68	15.7	0.250	5.50	0.345	38.4	44.2	301	9.59	1.12
W16 × 31 ⁴	9.13	15.9	0.275	5.53	0.440	47.2	54.0	375	12.4	1.17

Chapter 4 — Steel: Appendix

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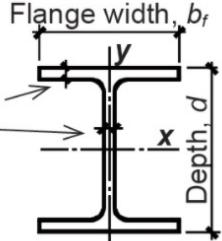
TOTAL LOAD DEFLECTION:

So, we can now compute the *actual* total load deflection:

$$\Delta = CP(L/12)^3 / (EI_x), \text{ or}$$

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Chapter 4 — Steel: Appendix

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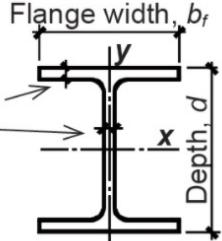
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	A500 Gr. B	42	58	HSS round ⁵
	A500 Gr. B	46	58	HSS rectangular ⁵
	A53 Gr. B	35	60	Pipe
High-strength, low-alloy	A992	50	65	³ W
	A572 Gr. 50	50	65	HP

Notes:

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TOTAL LOAD DEFLECTION:

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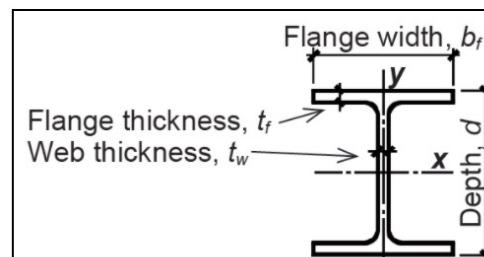
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For total loads (combined live and dead), the typical basic floor beam limit is **L/240** while typical roof beam limits are *L/120*, *L/180*, or *L/240* (for no ceiling, nonplaster ceiling, or plaster ceiling respectively).

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Chapter 4 — Steel: Appendix

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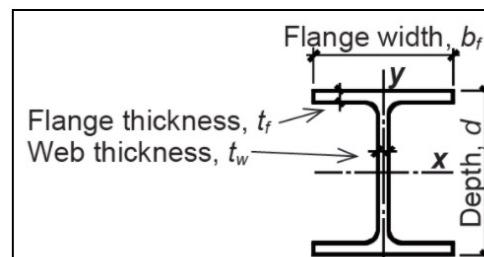
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Using the typical limit of L/240 (with L expressed in inches), we get an allowable value of $28 \times 12 / 240 = 1.4 \text{ in.}$

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Flange width, b_f
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Designa-tion	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
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Notes:

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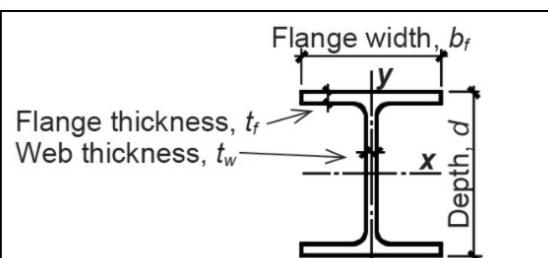
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Designa-tion	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
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Conclusion: Since the actual total-load deflection is greater than the allowable total-load deflection, the W16x26 is NOT OK for total-load deflection!

Chapter 4 — Steel: Appendix

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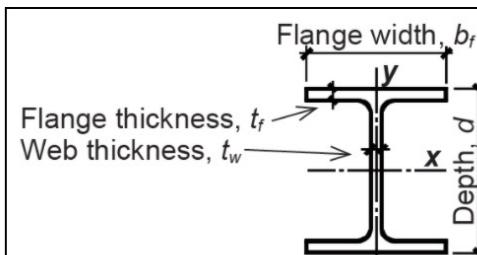
LIVE LOAD DEFLECTION...

is the same except with a different load in the equation.

The live load, $w = 75 \times 8 = 600\text{#/ft} = 0.6 \text{k/ft}$, so...

The live load, $P = 0.6 \times 28 = 16.8 \text{k}$

Table A-4.3: Dimensions and properties of steel W sections⁵



Cross-sectional area = A
 Moment of inertia = I
 Section modulus, $S_x = 2I_x/d$
 Sectional modulus, $S_y = 2I_x/b_f$
 Radius of gyration, $r_x = \sqrt{I_x/A}$
 Radius of gyration, $r_y = \sqrt{I_y/A}$

Designation	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W14 × 730	215	22.4	3.07	17.9	4.91	1280	1660	14300	4720	4.69
W14 × 808	238	22.8	3.74	18.6	5.12	1390	1830	15900	5550	4.83
W14 × 873	257	23.6	3.94	18.8	5.51	1530	2030	18100	6170	4.90
W16 × 26 ^{3,4}	7.68	15.7	0.250	5.50	0.345	38.4	44.2	301	9.59	1.12
W16 × 31 ⁴	9.13	15.9	0.275	5.53	0.440	47.2	54.0	375	12.4	1.17

Chapter 4 — Steel: Appendix

Table A-4.1: Steel properties¹

Category	ASTM designation	Yield stress, F_y (ksi)	(Ultimate) tensile stress, F_u (ksi)	Preferred for these shapes
Carbon	A36 A500 Gr. B A500 Gr. B A53 Gr. B	36 42 46 235	58 58 58 60	M, S, C, MC, L, plates ⁴ and bars HSS round ⁵ HSS rectangular ⁵ Pipe
High-strength, low-alloy	A992 A572 Gr. 50	50 50	65 65	³ W HP

Notes:

1. The modulus of elasticity, E , for these steels can be taken as 29,000 ksi.

LIVE LOAD DEFLECTION...

is the same except with a different load in the equation.

The live load, $w = 75 \times 8 = 600\text{#/ft} = 0.6 \text{k/ft}$, so...

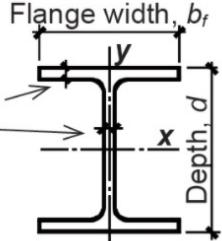
The live load, $P = 0.6 \times 28 = 16.8 \text{k}$

The *actual* live load deflection is:

$$\Delta = CP(L/12)^3 / (EI_x), \text{ or}$$

$$\Delta = (22.46)(16.8)(28)^3 / (29,000 \times 301) = 0.95 \text{ in.}$$

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Cross-sectional area = A
 Moment of inertia = I
 Section modulus, $S_x = 2I_x/d$
 Sectional modulus, $S_y = 2I_x/b_f$
 Radius of gyration, $r_x = \sqrt{I_x/A}$
 Radius of gyration, $r_y = \sqrt{I_y/A}$

Designa-tion	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
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The live load, $P = 0.6 \times 28 = 16.8 \text{k}$

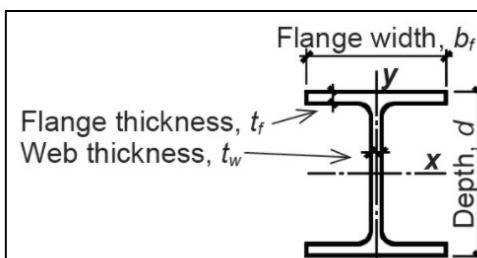
The *actual* live load deflection is:

$$\Delta = CP(L/12)^3 / (EI_x), \text{ or}$$

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The *allowable* live load deflection can be found in the footnotes to Table A-4.17 (or A-3.15):

Table A-4.3: Dimensions and properties of steel W sections⁵



Flange width, b_f
Flange thickness, t_f
Web thickness, t_w
Depth, d

Cross-sectional area = A
Moment of inertia = I
Section modulus, $S_x = 2I_x/d$
Sectional modulus, $S_y = 2I_y/b_f$
Radius of gyration, $r_x = \sqrt{I_x/A}$
Radius of gyration, $r_y = \sqrt{I_y/b_f}$

Designa-tion	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W14 × 730	215	22.4	3.07	17.9	4.91	1280	1660	14300	4720	4.69
W14 × 808	238	22.8	3.74	18.6	5.12	1390	1830	15900	5550	4.83
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Chapter 4 — Steel: Appendix

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The *actual* live load deflection is:

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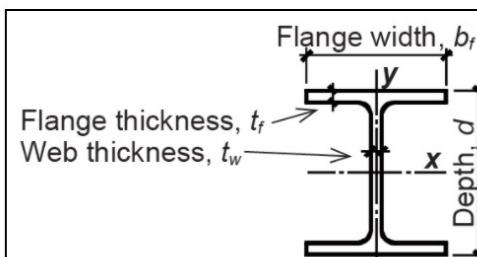
$$\Delta = (22.46)(16.8)(28)^3 / (29,000 \times 301) = 0.95 \text{ in.}$$

The *allowable* live load deflection can be found in the footnotes to Table A-4.17 (or A-3.15):

For live loads only, the typical basic floor beam limit is $L/360$ while typical roof beam limits are $L/180$, $L/240$, or $L/360$ (for no ceiling, nonplaster ceiling, or plaster ceiling respectively).

Using the typical limit of $L/360$ (with L expressed in inches), we get an allowable value of $28 \times 12 / 360 = 0.93 \text{ in.}$

Table A-4.3: Dimensions and properties of steel W sections⁵



Cross-sectional area = A
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 Section modulus, $S_x = 2I_x/d$
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 Radius of gyration, $r_x = \sqrt{I_x/A}$
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Designa-tion	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
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Notes:

1. The modulus of elasticity, E , for these steels can be taken as 29,000 ksi.

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The live load, $w = 75 \times 8 = 600\#/ft = 0.6 \text{ k/ft}$, so...

The live load, $P = 0.6 \times 28 = 16.8 \text{ k}$

The *actual* live load deflection is:

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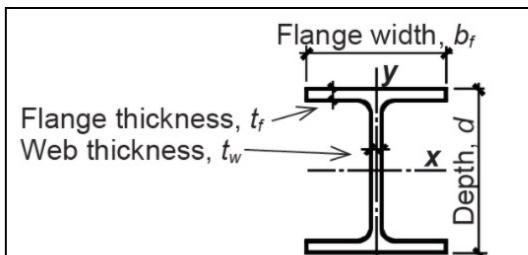
The *allowable* live load deflection can be found in the footnotes to Table A-4.17 (or A-3.15):

For live loads only, the typical basic floor beam limit is $L/360$ while typical roof beam limits are $L/180$, $L/240$, or $L/360$ (for no ceiling, nonplaster ceiling, or plaster ceiling respectively).

Using the typical limit of $L/360$ (with L expressed in inches), we get an allowable value of $28 \times 12 / 360 = 0.93 \text{ in.}$

Conclusion: Since the actual total-load deflection is greater than the allowable total-load deflection, the W16x26 is NOT OK for live-load deflection!

Table A-4.3: Dimensions and properties of steel W sections⁵



Cross-sectional area = A
 Moment of inertia = I
 Section modulus, $S_x = 2I_x/d$
 Sectional modulus, $S_y = 2I_x/b_f$
 Radius of gyration, $r_x = \sqrt{I_x/A}$
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Designa-tion	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
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Chapter 4 — Steel: Appendix

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Notes:

1. The modulus of elasticity, E , for these steels can be taken as 29,000 ksi.

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The live load, $w = 75 \times 8 = 600\#/ft = 0.6 \text{ k/ft}$, so...

The live load, $P = 0.6 \times 28 = 16.8 \text{ k}$

The *actual* live load deflection is:

$$\Delta = CP(L/12)^3 / (EI_x), \text{ or}$$

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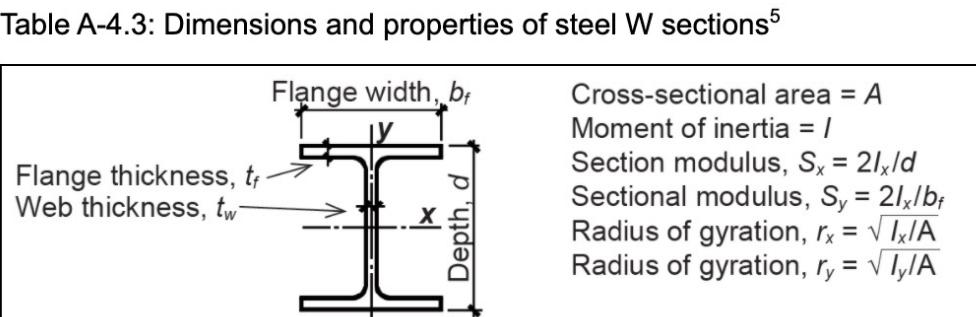
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For live loads only, the typical basic floor beam limit is $L/360$ while typical roof beam limits are $L/180$, $L/240$, or $L/360$ (for no ceiling, nonplaster ceiling, or plaster ceiling respectively).

Using the typical limit of $L/360$ (with L expressed in inches), we get an allowable value of $28 \times 12 / 360 = 0.93 \text{ in.}$

Conclusion: Since the actual total-load deflection is greater than the allowable total-load deflection, the W16x26 is not OK for live-load deflection!

To improve the deflection performance of the beam, find a cross section with a larger moment of inertia (and an acceptable plastic section modulus for bending stress).



Designa-tion	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W14 × 730	215	22.4	3.07	17.9	4.91	1280	1660	14300	4720	4.69
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Chapter 4 — Steel: Appendix

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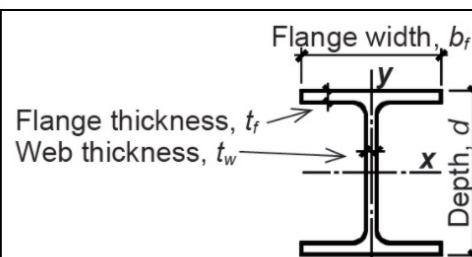
Using the typical limit of $L/360$ (with L expressed in inches), we get an allowable value of $28 \times 12 / 360 = 0.93 \text{ in.}$

Conclusion: Since the actual total-load deflection is greater than the allowable total-load deflection, the W16x26 is not OK for live-load deflection!

To improve the deflection performance of the beam, find a cross section with a larger moment of inertia (and an acceptable plastic section modulus for bending stress).

But we will not redesign this beam: only note that it is not OK for live load deflection (but it's close).

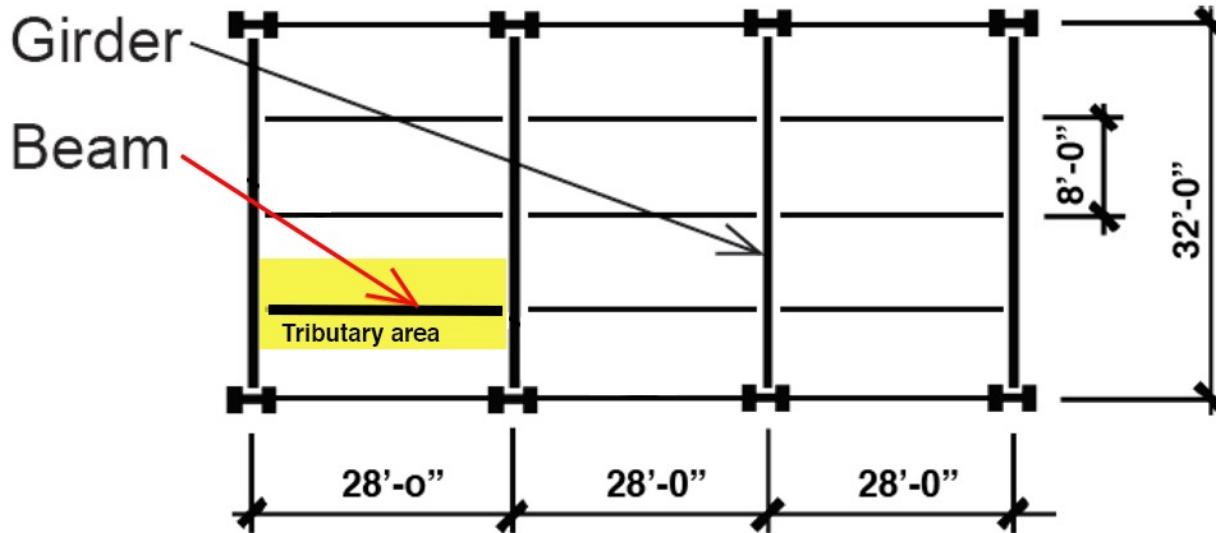
Table A-4.3: Dimensions and properties of steel W sections⁵



Flange width, b_f
Flange thickness, t_f
Web thickness, t_w
Depth, d

Cross-sectional area = A
Moment of inertia = I
Section modulus, $S_x = 2I_x/d$
Sectional modulus, $S_y = 2I_x/b_f$
Radius of gyration, $r_x = \sqrt{I_x/A}$
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Designa-tion	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
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W16 × 31 ⁴	9.13	15.9	0.275	5.53	0.440	47.2	54.0	375	12.4	1.17



Framing plan

Design typical beam (no live load reduction).

Assume L = 75 psf and D = 55 psf

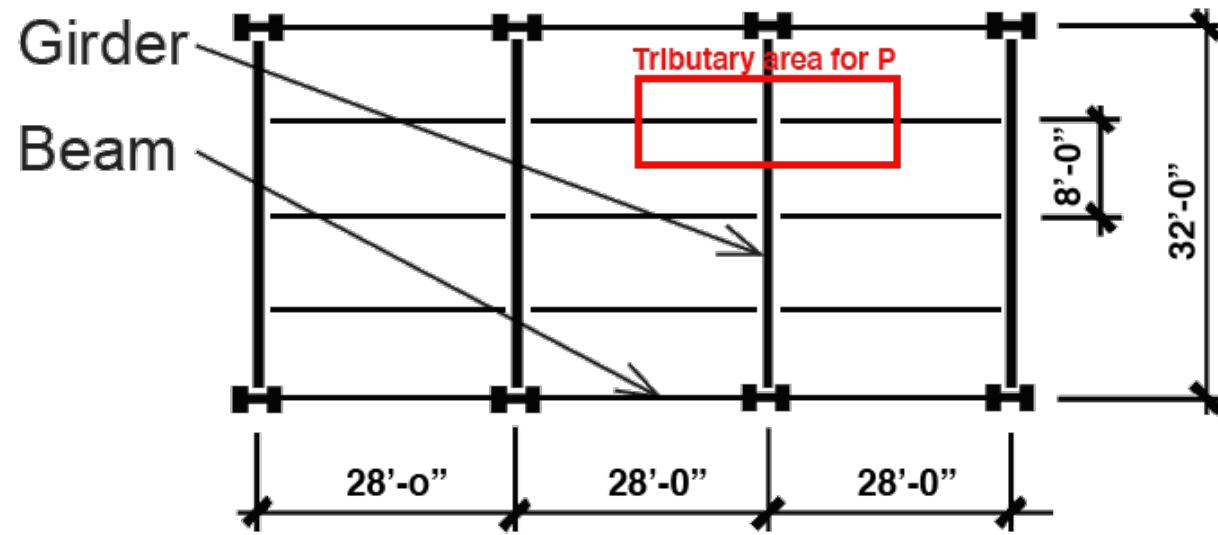
Use A-992 steel with $F_y = 50$ ksi

Just for the record, if we were going to account for live load reduction, we would use a tributary area = $28 \times 8 = 224 \text{ ft}^2$ and a live load element factor, $K_{LL} = 2$.

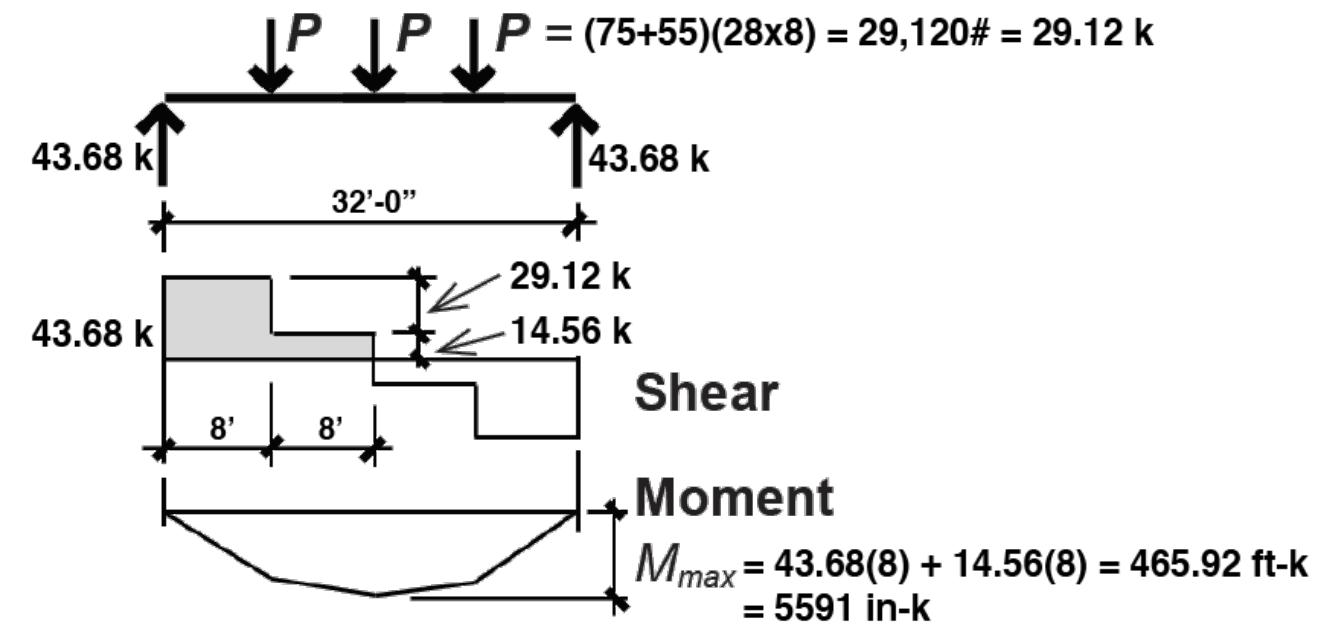
The reduced live load would therefore be $75 \times [0.25 + 15 / \sqrt{2 \times 224}] = 75 \times 0.96 = \text{71.9 psf}$

But, for this example, we used the unreduced live load, L = 75 psf...

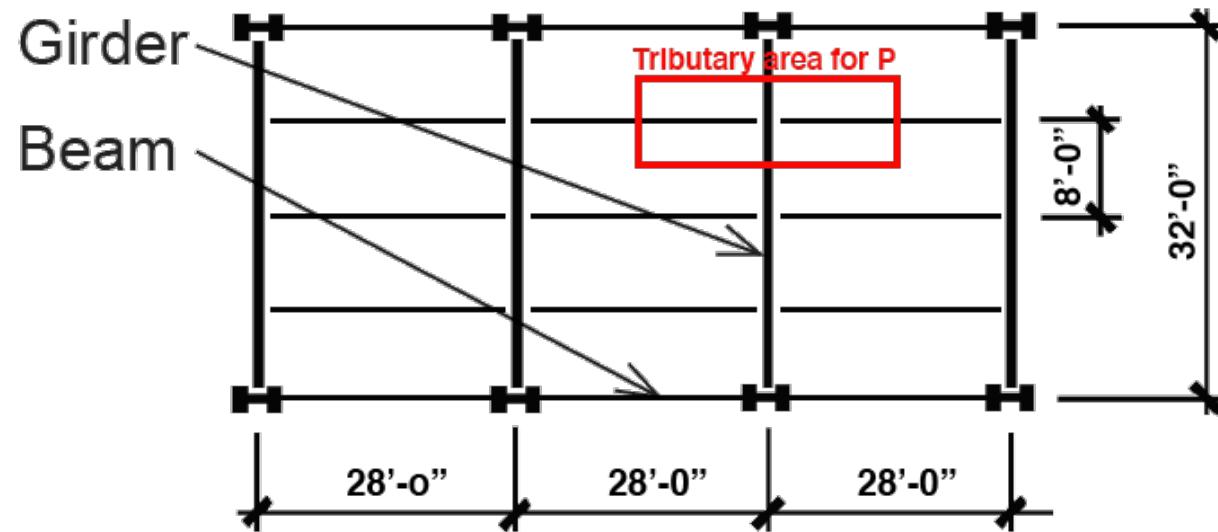
Now, on to girder design, also using the unreduced live load.



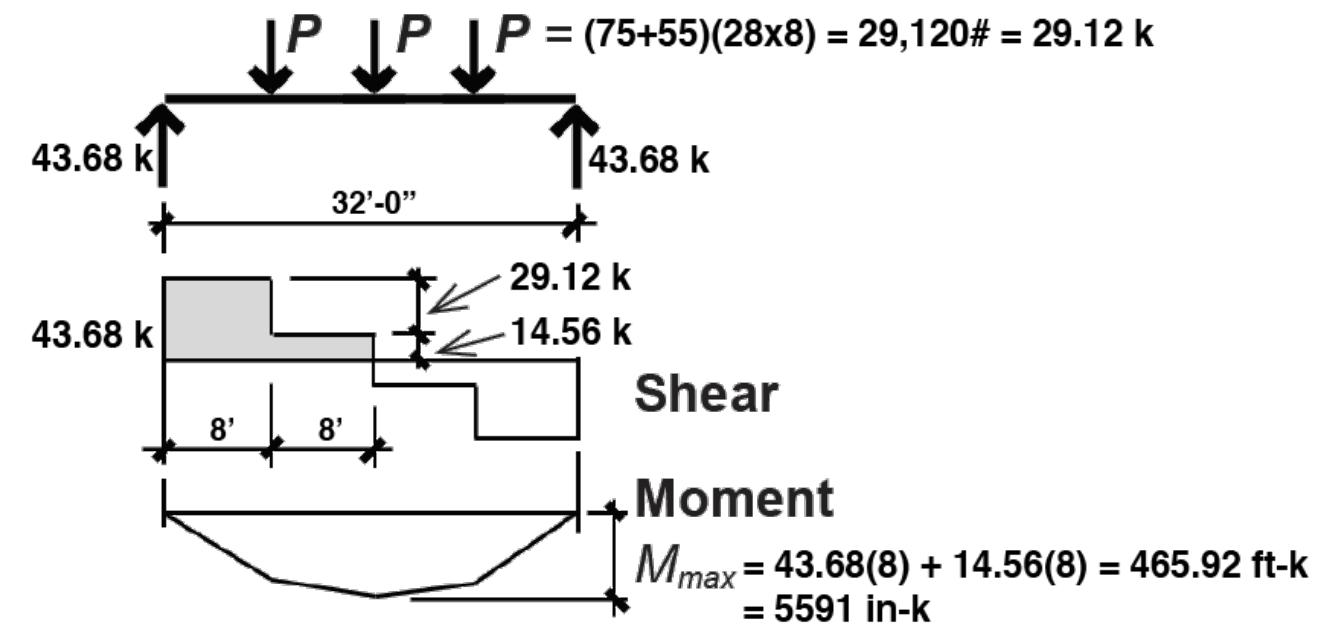
Framing plan



Design typical girder (no live load reduction).



Framing plan



Design typical girder (no live load reduction).

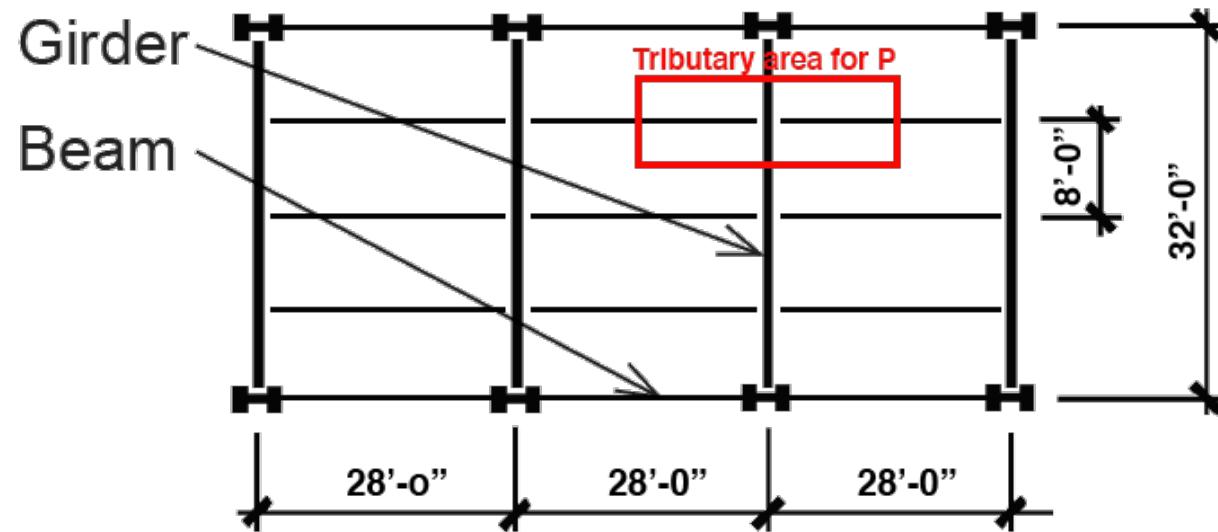
Assume L = 75 psf and D = 55 psf

Use A-992 steel with $F_y = 50$ ksi

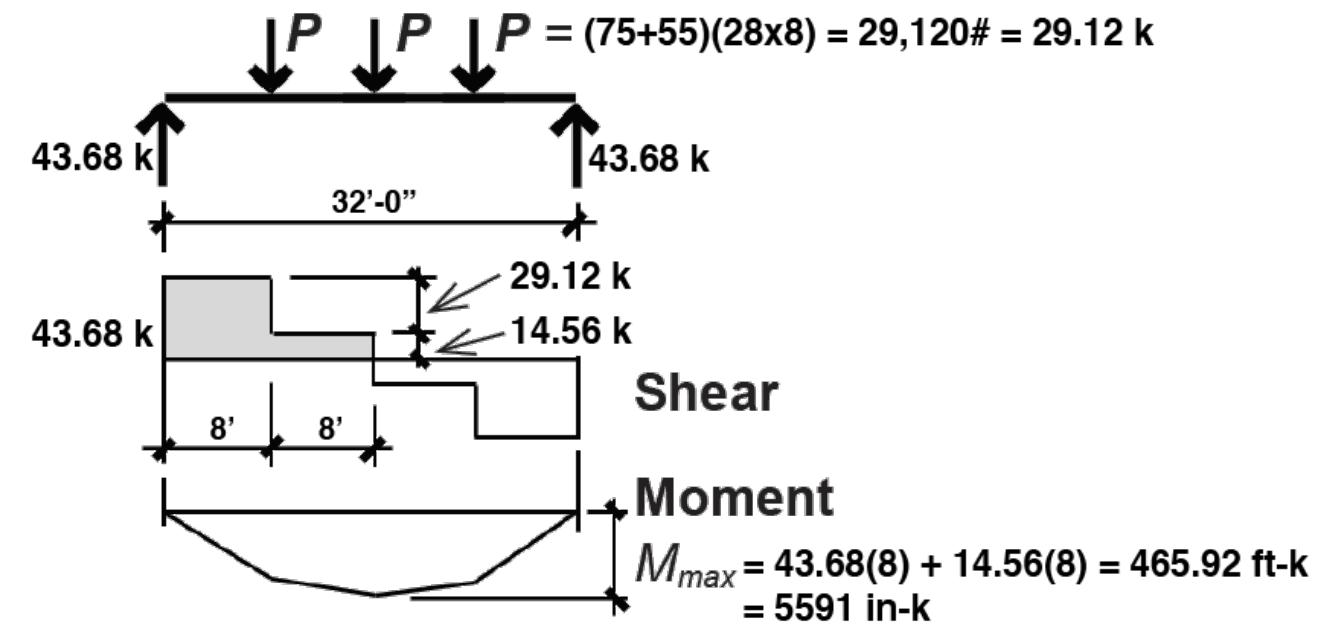
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Table A-4.1: Steel properties¹

Category	ASTM designation	Yield stress, F_y (ksi)	(Ultimate) tensile stress, F_u (ksi)	Preferred for these shapes
Carbon	A36	36	58	M, S, C, MC, L, plates ⁴ and bars
	A500 Gr. B	42	58	HSS round ⁵
	A500 Gr. B	46	58	HSS rectangular ⁵
	A53 Gr. B	35	60	Pipe
High-strength, low-alloy	A992	50	65	³ W
	A572 Gr. 50	50	65	HP



Framing plan



Design typical girder (no live load reduction).

Assume L = 75 psf and D = 55 psf

Use A-992 steel with $F_y = 50 \text{ ksi}$

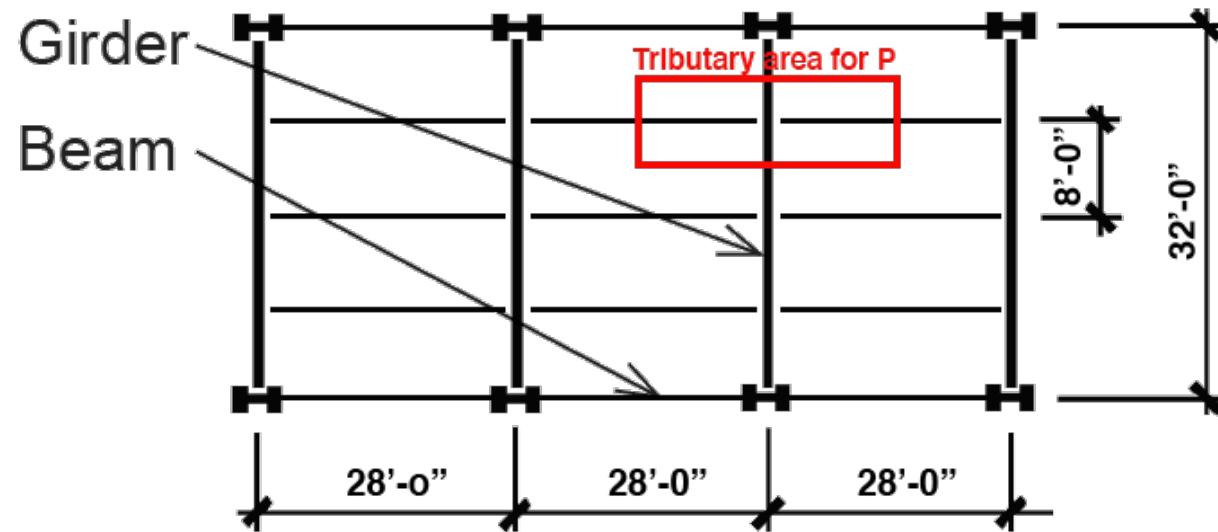
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$$Z_{req} = M_{max} / (0.6F_y)$$

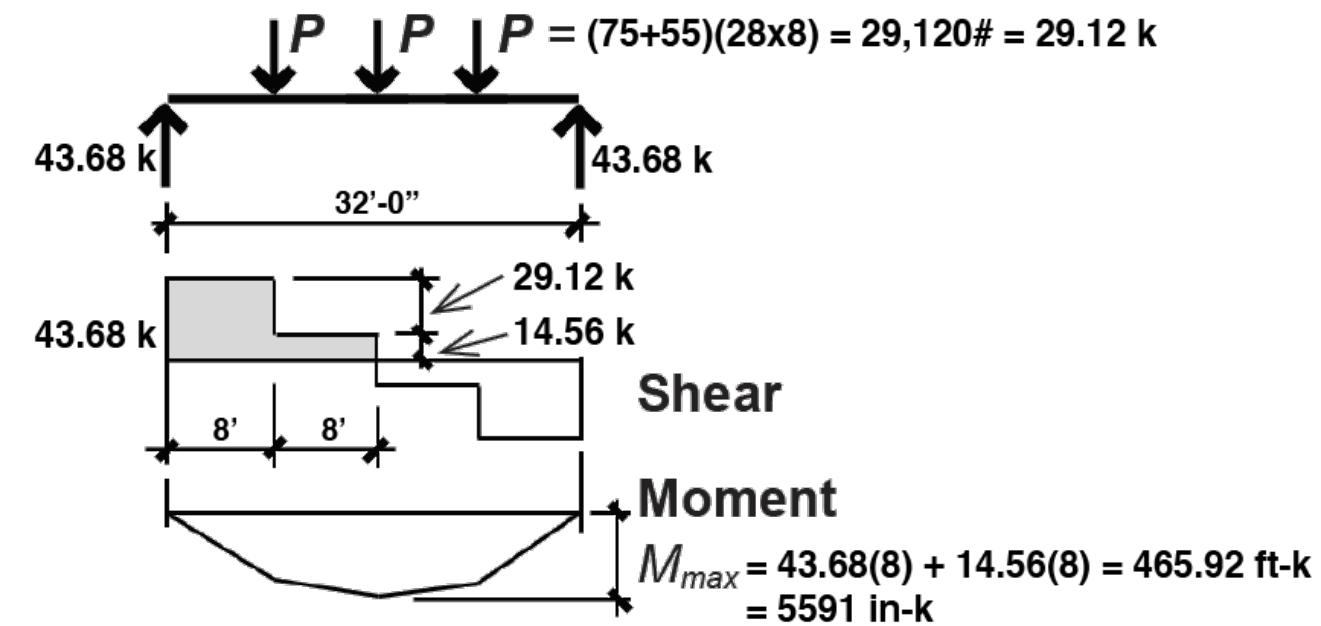
Table A-4.1: Steel properties¹

$$Z_{req} = 5591 / (0.6 \times 50) = 186.4 \text{ in}^3$$

Category	ASTM designation	Yield stress, F_y (ksi)	(Ultimate) tensile stress, F_u (ksi)	Preferred for these shapes
Carbon	A36	36	58	M, S, C, MC, L, plates ⁴ and bars
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High-strength, low-alloy	A992	50	65	³ W
	A572 Gr. 50	50	65	HP



Framing plan



Design typical girder (no live load reduction).

Assume L = 75 psf and D = 55 psf

Use A-992 steel with $F_y = 50 \text{ ksi}$

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$$Z_{req} = M_{max} / (0.6F_y)$$

$$Z_{req} = 5591 / (0.6 \times 50) = 186.4 \text{ in}^3$$

Select provisional section from Table A-4.15

Table A-4.1: Steel properties¹

Category	ASTM designation	Yield stress, F_y (ksi)	(Ultimate) tensile stress, F_u (ksi)	Preferred for these shapes
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	A53 Gr. B	35	60	Pipe
High-strength, low-alloy	A992	50	65	³ W
	A572 Gr. 50	50	65	HP

From Table A-4.15, select lightest section with a plastic section modulus of at least 186.4 in³

Select a W24x76

Table A-4.15: Plastic section modulus (Z_x) values: lightest laterally braced steel compact shapes for bending, $F_y = 50$ ksi

Shape	Z_x (in ³)	2L_p (ft)	Shape	Z_x (in ³)	2L_p (ft)	Shape	Z_x (in ³)	2L_p (ft)
W6 × 8.5 ¹	5.59	3.14	W21 × 55	126	6.11	W40 × 211	906	8.87
W6 × 9 ¹	6.23	3.20	W24 × 55	134	4.73	W40 × 215	964	12.5
W8 × 10 ¹	8.77	3.14	W21 × 62	144	6.25	W44 × 230	1100	12.1
W10 × 12 ¹	12.5	2.87	W24 × 62	153	4.87	W40 × 249	1120	12.5
W12 × 14	17.4	2.66	W21 × 68	160	6.36	W44 × 262	1270	12.3
W12 × 16	20.1	2.73	W24 × 68	177	6.61	W44 × 290	1410	12.3
W10 × 19	21.6	3.09	W24 × 76	200	6.78	W40 × 324	1460	12.6
W12 × 19	24.7	2.90	W24 × 84	224	6.89	W44 × 335	1620	12.3
W10 × 22	26.0	4.70	W27 × 84	244	7.31	W40 × 362	1640	12.7
W12 × 22	29.3	3.00	W30 × 90	283	7.38	W40 × 372	1680	12.7
W14 × 22	33.2	3.67	W30 × 99	312	7.42	W40 × 392	1710	9.33
W12 × 26	37.2	5.33	W30 × 108	346	7.59	W40 × 397	1800	12.9
W14 × 26	40.2	3.81	W30 × 116	378	7.74	W40 × 431	1960	12.9
W16 × 26	44.2	3.96	W33 × 118	415	8.19	W36 × 487	2130	14.0
W14 × 30	47.3	5.26	W33 × 130	467	8.44	W40 × 503	2320	13.1
W16 × 31	54.0	4.13	W36 × 135	509	8.41	W36 × 529	2330	14.1
W14 × 34	54.6	5.40	W33 × 141	514	8.58	W40 × 593	2760	13.4
W18 × 35	66.5	4.31	W40 × 149	598	8.09	W36 × 652	2910	14.5
W16 × 40	73.0	5.55	W36 × 160	624	8.83	W36 × 655	3080	13.6
W18 × 40	78.4	4.49	W40 × 167	693	8.48	W36 × 723	3270	14.7
W21 × 44	95.4	4.45	W36 × 182	718	9.01	W36 × 802	3660	14.9
W21 × 48	107	6.09	W40 × 183	774	8.80	W36 × 853	3920	15.1
W21 × 50	110	4.59	W40 × 199	869	12.2	W36 × 925	4130	15.0
W18 × 55	112	5.90						

From Table A-4.15, select lightest section with a plastic section modulus of at least 186.4 in³

Select a W24x76

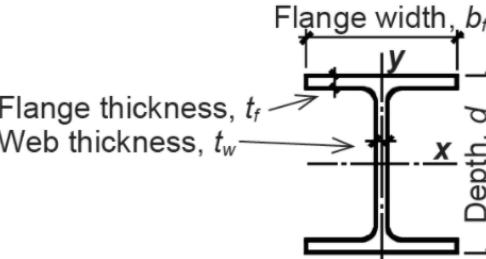
Now, check for shear and deflection:

Table A-4.15: Plastic section modulus (Z_x) values: lightest laterally braced steel compact shapes for bending, $F_y = 50$ ksi

Shape	Z_x (in ³)	2L_p (ft)	Shape	Z_x (in ³)	2L_p (ft)	Shape	Z_x (in ³)	2L_p (ft)
W6 × 8.5 ¹	5.59	3.14	W21 × 55	126	6.11	W40 × 211	906	8.87
W6 × 9 ¹	6.23	3.20	W24 × 55	134	4.73	W40 × 215	964	12.5
W8 × 10 ¹	8.77	3.14	W21 × 62	144	6.25	W44 × 230	1100	12.1
W10 × 12 ¹	12.5	2.87	W24 × 62	153	4.87	W40 × 249	1120	12.5
W12 × 14	17.4	2.66	W21 × 68	160	6.36	W44 × 262	1270	12.3
W12 × 16	20.1	2.73	W24 × 68	177	6.61	W44 × 290	1410	12.3
W10 × 19	21.6	3.09	W24 × 76	200	6.78	W40 × 324	1460	12.6
W12 × 19	24.7	2.90	W24 × 84	224	6.89	W44 × 335	1620	12.3
W10 × 22	26.0	4.70	W27 × 84	244	7.31	W40 × 362	1640	12.7
W12 × 22	29.3	3.00	W30 × 90	283	7.38	W40 × 372	1680	12.7
W14 × 22	33.2	3.67	W30 × 99	312	7.42	W40 × 392	1710	9.33
W12 × 26	37.2	5.33	W30 × 108	346	7.59	W40 × 397	1800	12.9
W14 × 26	40.2	3.81	W30 × 116	378	7.74	W40 × 431	1960	12.9
W16 × 26	44.2	3.96	W33 × 118	415	8.19	W36 × 487	2130	14.0
W14 × 30	47.3	5.26	W33 × 130	467	8.44	W40 × 503	2320	13.1
W16 × 31	54.0	4.13	W36 × 135	509	8.41	W36 × 529	2330	14.1
W14 × 34	54.6	5.40	W33 × 141	514	8.58	W40 × 593	2760	13.4
W18 × 35	66.5	4.31	W40 × 149	598	8.09	W36 × 652	2910	14.5
W16 × 40	73.0	5.55	W36 × 160	624	8.83	W36 × 655	3080	13.6
W18 × 40	78.4	4.49	W40 × 167	693	8.48	W36 × 723	3270	14.7
W21 × 44	95.4	4.45	W36 × 182	718	9.01	W36 × 802	3660	14.9
W21 × 48	107	6.09	W40 × 183	774	8.80	W36 × 853	3920	15.1
W21 × 50	110	4.59	W40 × 199	869	12.2	W36 × 925	4130	15.0
W18 × 55	112	5.90						

We find section properties for the **W24x76** beam in Table A-4.3.

Table A-4.3: Dimensions and properties of steel W sections⁵



Designa-tion	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W24 × 68 ⁴	20.1	23.7	0.415	8.97	0.585	154	177	1830	70.4	1.87
W24 × 76 ⁴	22.4	23.9	0.440	8.99	0.680	176	200	2100	82.5	1.92
W24 × 84 ⁴	24.7	24.1	0.470	9.02	0.770	196	224	2370	94.4	1.95
W24 × 94 ⁴	27.7	24.3	0.515	9.07	0.875	222	254	2700	109	1.98
W24 × 103 ⁴	30.3	24.5	0.550	9.00	0.980	245	280	3000	119	1.99

Notes:

1. Section not compact for steel with $F_y = 36$ ksi or $F_y = 50$ ksi.
2. Section compact for steel with $F_y = 36$ ksi, but not compact for steel with $F_y = 50$ ksi.
3. Section webs do not meet slenderness criteria for shear for which the allowable stress can be taken as $F_v = 0.4F_y$; instead, use a reduced allowable shear stress, $F_v = 0.36F_y$.
4. Section is slender for compression with $F_y = 50$ ksi.
5. W-shapes are grouped together with common inner roller dimensions (i.e., web "lengths" excluding fillets)

We find section properties for the **W24x76** beam in Table A-4.3.

This is also where we find out whether to use a safety factor of **0.4** or **0.36**.

Without footnote 3 marked next to the section, we use a safety factor of **4.0**.

Table A-4.3: Dimensions and properties of steel W sections⁵

Designa-tion	A (in ²)	d (in.)	t _w (in.)	b _f (in.)	t _f (in.)	S _x (in ³)	Z _x (in ³)	I _x (in ⁴)	I _y (in ⁴)	r _y (in.)
W24 × 68 ⁴	20.1	23.7	0.415	8.97	0.585	154	177	1830	70.4	1.87
W24 × 76 ⁴	22.4	23.9	0.440	8.99	0.680	176	200	2100	82.5	1.92
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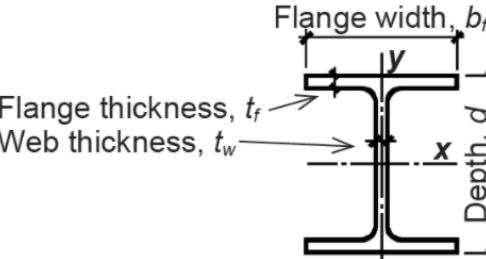
We find section properties for the **W24x76** beam in Table A-4.3.

This is also where we find out whether to use a safety factor of **0.4** or **0.36**.

Without footnote 3 marked next to the section, we use a safety factor of **4.0**.

Since $V = 43.68 \text{ k}$ and $F_y = 50 \text{ ksi}$, the required web area, $A_w = 43.68 / (0.40 \times 50) = 2.184 \text{ in}^2$

Table A-4.3: Dimensions and properties of steel W sections⁵



Designation	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W24 x 68 ⁴	20.1	23.7	0.415	8.97	0.585	154	177	1830	70.4	1.87
W24 x 76 ⁴	22.4	23.9	0.440	8.99	0.680	176	200	2100	82.5	1.92
W24 x 84 ⁴	24.7	24.1	0.470	9.02	0.770	196	224	2370	94.4	1.95
W24 x 94 ⁴	27.7	24.3	0.515	9.07	0.875	222	254	2700	109	1.98
W24 x 103 ⁴	30.3	24.5	0.550	9.00	0.980	245	280	3000	119	1.99

Notes:

1. Section not compact for steel with $F_y = 36 \text{ ksi}$ or $F_y = 50 \text{ ksi}$.
2. Section compact for steel with $F_y = 36 \text{ ksi}$, but not compact for steel with $F_y = 50 \text{ ksi}$.
3. Section webs do not meet slenderness criteria for shear for which the allowable stress can be taken as $F_v = 0.4F_y$; instead, use a reduced allowable shear stress, $F_v = 0.36F_y$.
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5. W-shapes are grouped together with common inner roller dimensions (i.e., web "lengths" excluding fillets)

We find section properties for the **W24x76** beam in Table A-4.3.

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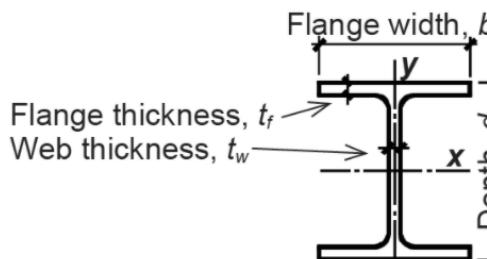
Without footnote 3 marked next to the section, we use a safety factor of **4.0**.

Since $V = 43.68 \text{ k}$ and $F_y = 50 \text{ ksi}$, the required web area, $A_w = 43.68 / (0.40 \times 50) = 2.184 \text{ in}^2$

We compare this required web area to the actual web area by finding d and t_w in **Table A-4.3**.

$d = 23.9 \text{ in.}$ and $t_w = 0.44 \text{ in.}$ Therefore, the actual web area = $23.9 \times 0.44 = 10.52 \text{ in}^2$.

Table A-4.3: Dimensions and properties of steel W sections⁵



Designa-tion	A (in2)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in3)	Z_x (in3)	I_x (in4)	I_y (in4)	r_y (in.)
W24 × 68⁴	20.1	23.7	0.415	8.97	0.585	154	177	1830	70.4	1.87
W24 × 76⁴	22.4	23.9	0.440	8.99	0.680	176	200	2100	82.5	1.92
W24 × 84⁴	24.7	24.1	0.470	9.02	0.770	196	224	2370	94.4	1.95
W24 × 94⁴	27.7	24.3	0.515	9.07	0.875	222	254	2700	109	1.98
W24 × 103⁴	30.3	24.5	0.550	9.00	0.980	245	280	3000	119	1.99

Notes:

1. Section not compact for steel with $F_y = 36 \text{ ksi}$ or $F_y = 50 \text{ ksi}$.
2. Section compact for steel with $F_y = 36 \text{ ksi}$, but not compact for steel with $F_y = 50 \text{ ksi}$.
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4. Section is slender for compression with $F_y = 50 \text{ ksi}$.
5. W-shapes are grouped together with common inner roller dimensions (i.e., web "lengths" excluding fillets)

We find section properties for the **W24x76** beam in Table A-4.3.

This is also where we find out whether to use a safety factor of **0.4** or **0.36**.

Without footnote 3 marked next to the section, we use a safety factor of **4.0**.

Since $V = 43.68 \text{ k}$ and $F_y = 50 \text{ ksi}$, the required web area, $A_w = 43.68 / (0.40 \times 50) = 2.184 \text{ in}^2$

We compare this required web area to the actual web area by finding d and t_w in **Table A-4.3**.

$d = 23.9 \text{ in.}$ and $t_w = 0.44 \text{ in.}$ Therefore, the actual web area = $23.9 \times 0.44 = 10.52 \text{ in}^2$.

Since the actual web area is greater or equal to the required web area, **the section is OK for shear.**

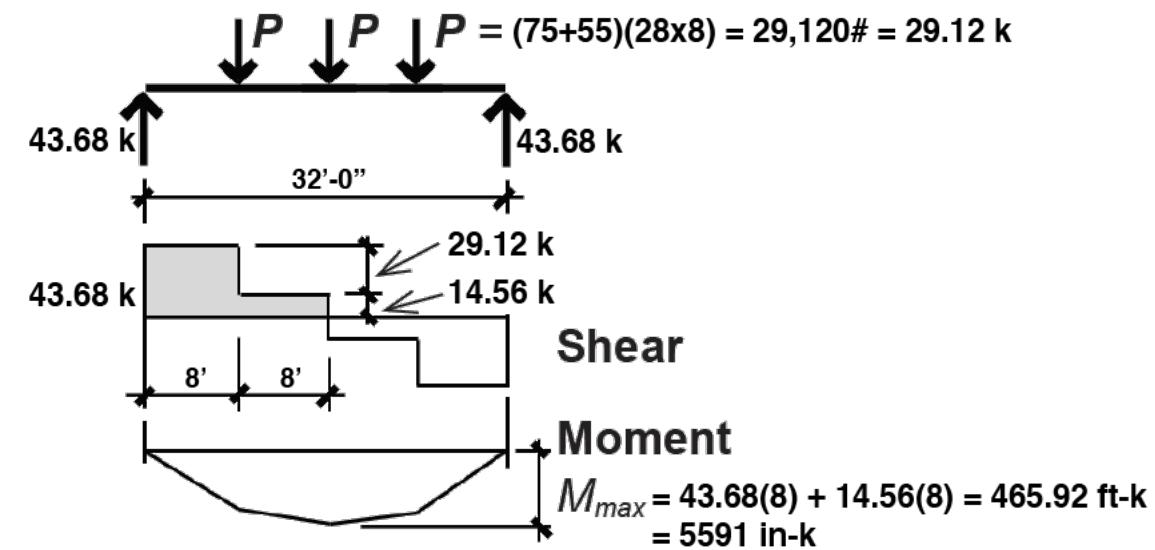
Table A-4.3: Dimensions and properties of steel W sections⁵

Designa-tion	A (in 2)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in 3)	Z_x (in 3)	I_x (in 4)	I_y (in 4)	r_y (in.)
						Cross-sectional area = A	Moment of inertia = I	Section modulus, $S_x = 2I_x/d$	Sectional modulus, $S_y = 2I_x/b_f$	Radius of gyration, $r_x = \sqrt{I_x/A}$
W24 × 68 ⁴	20.1	23.7	0.415	8.97	0.585	154	177	1830	70.4	1.87
W24 × 76 ⁴	22.4	23.9	0.440	8.99	0.680	176	200	2100	82.5	1.92
W24 × 84 ⁴	24.7	24.1	0.470	9.02	0.770	196	224	2370	94.4	1.95
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Notes:

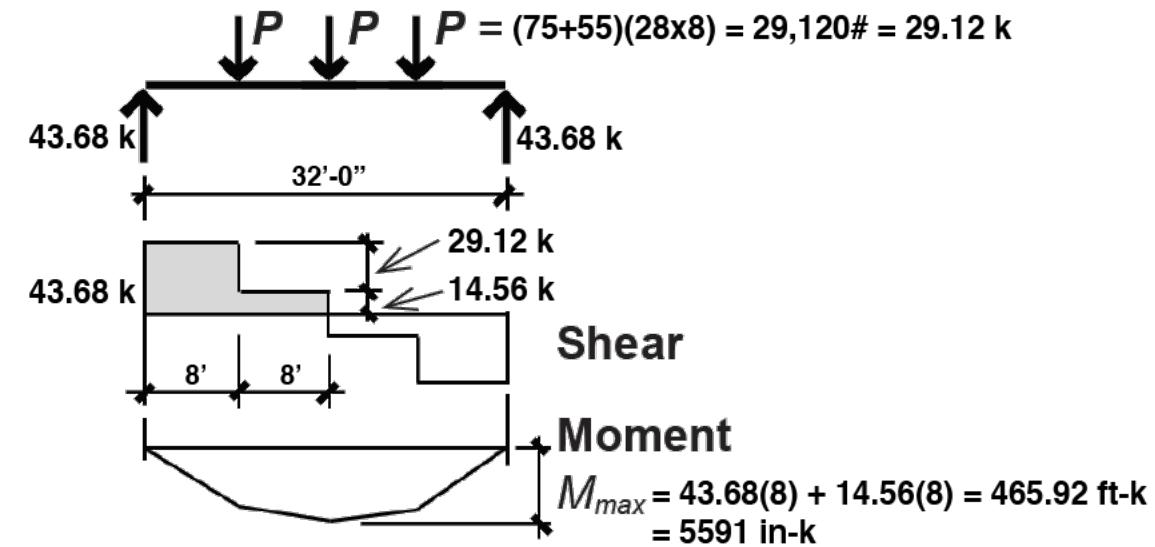
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5. W-shapes are grouped together with common inner roller dimensions (i.e., web "lengths" excluding fillets)

The last step in the beam design process is to **check the W24x76 for deflection.**



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Here, the relevant parameters are material properties (modulus of elasticity, E), sectional properties (moment of inertia, I_x), span (L), and load (w).

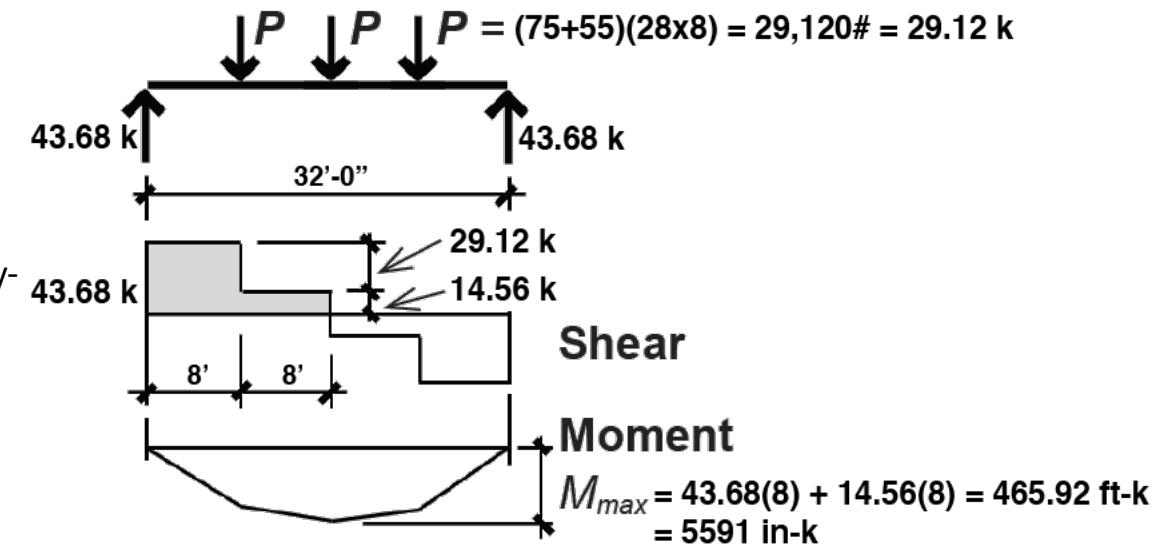


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Here, the relevant parameters are material properties (modulus of elasticity, E), sectional properties (moment of inertia, I_x), span (L), and load (w).

Rather than using the specialized equation for maximum mid-span deflection of a uniformly-loaded simply-supported beams, which is:

$$\Delta = 5wL^4 / (384EI_x)$$



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We'll use the equation from the more flexible Appendix Table A-4.17 (same as A-3.15):

$$\Delta = CP(L/12)^3 / (EI_x) \text{ where the coefficient, } C \text{ is found from the table: } C = 85.54 \text{ in this case.}$$

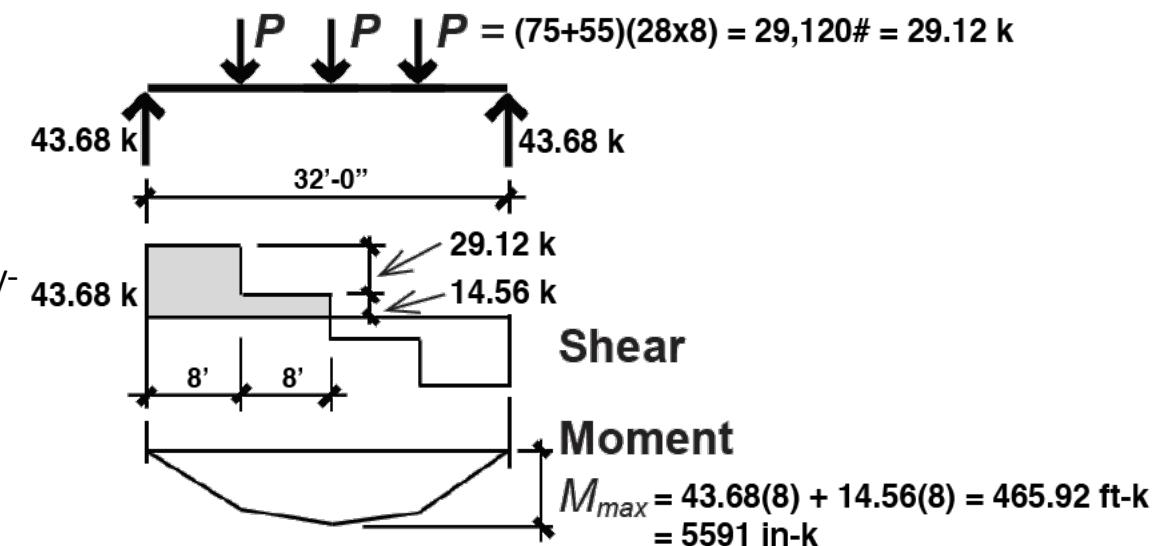


Table A-4.17: Maximum (actual) deflection in a beam^{1,2,3}

Deflection coefficient, C , for maximum (actual) deflection, Δ (in.), where $\Delta = \frac{CP(L/12)^3}{EI_x}$				
$P = w(L/12)$	22.46	9.33	4.49	216
	35.94	16.07	8.99	n/a
	61.34	26.27	13.31	n/a
	85.54	36.12	17.97	n/a
	n/a	n/a	n/a	576

The last step in the beam design process is to **check the W24x76 for deflection**.

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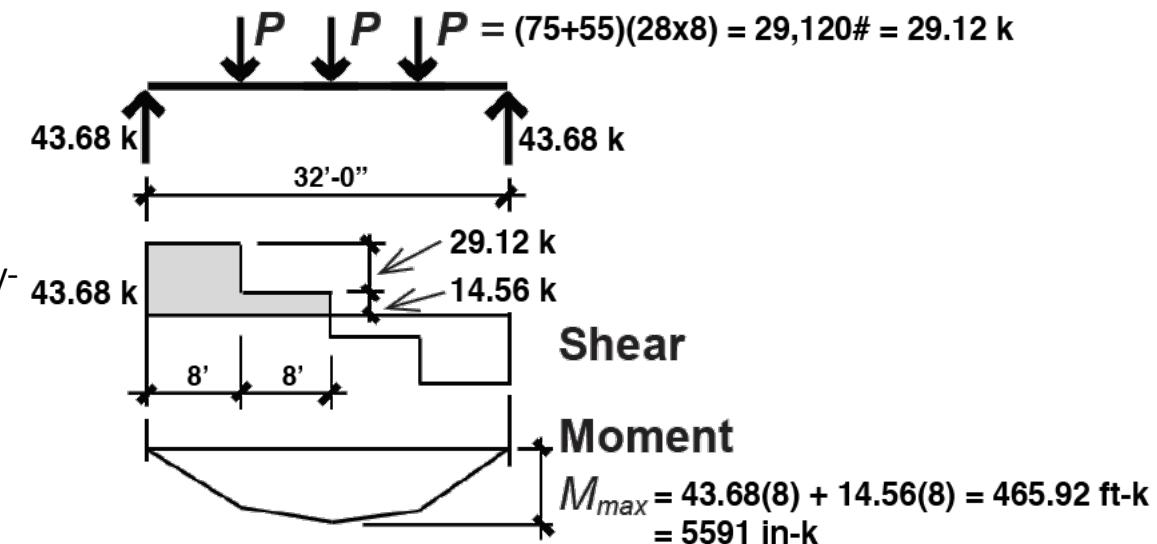


Table A-4.17: Maximum (actual) deflection in a beam^{1,2,3}

Deflection coefficient, C , for maximum (actual) deflection, Δ (in.), where $\Delta = \frac{CP(L/12)^3}{EI_x}$				
$P = w(L/12)$	22.46	9.33	4.49	216
	35.94	16.07	8.99	n/a
	61.34	26.27	13.31	n/a
	85.54	36.12	17.97	n/a
	n/a	n/a	n/a	576

The other parameters are easily determined:

$P = 29.12 \text{ k}$ for total load deflection (from diagram); and
 $P = (75)(28x8) = 16,800\# = 16.8 \text{ k}$ for live load deflection

The last step in the beam design process is to **check the W24x76 for deflection**.

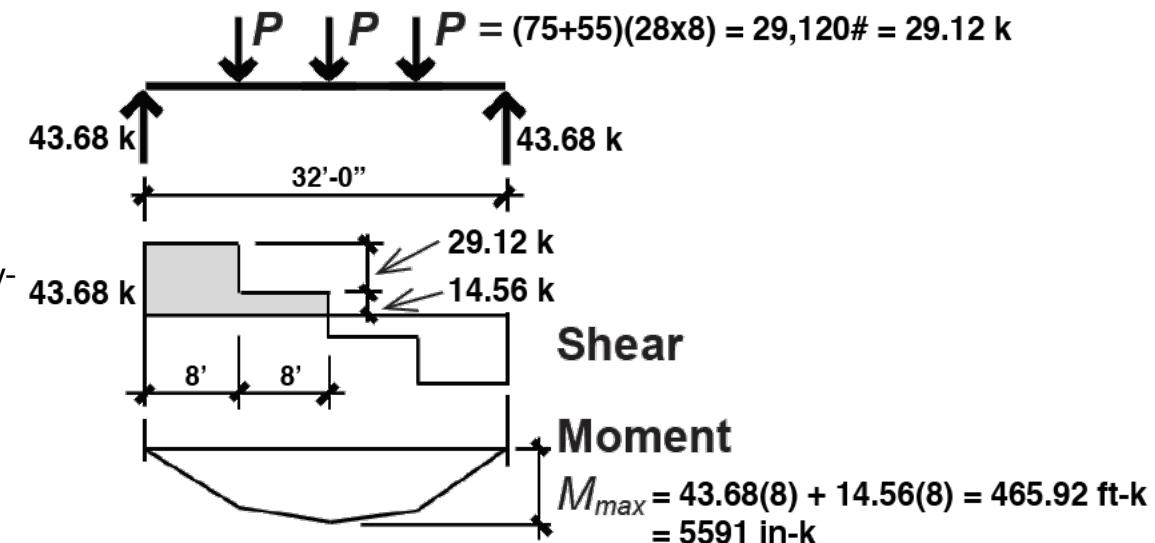
Here, the relevant parameters are material properties (modulus of elasticity, E), sectional properties (moment of inertia, I_x), span (L), and load (w).

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$$\Delta = CP(L/12)^3 / (EI_x) \text{ where the coefficient, } C \text{ is found from the table: } C = 85.54 \text{ in this case.}$$



$$M_{max} = 43.68(8) + 14.56(8) = 465.92 \text{ ft-k} \\ = 5591 \text{ in-k}$$

Table A-4.17: Maximum (actual) deflection in a beam^{1,2,3}

Deflection coefficient, C , for maximum (actual) deflection, Δ (in.), where $\Delta = \frac{CP(L/12)^3}{EI_x}$				
$P = w(L/12)$	22.46	9.33	4.49	216
	35.94	16.07	8.99	n/a
	61.34	26.27	13.31	n/a
	85.54	36.12	17.97	n/a
	n/a	n/a	n/a	576

The other parameters are easily determined:

$P = 29.12 \text{ k}$ for total load deflection (from diagram); and
 $P = (75)(28x8) = 16,800\# = 16.8 \text{ k}$ for live load deflection

Start with total load deflection.

Chapter 4 — Steel: Appendix

TOTAL LOAD DEFLECTION:

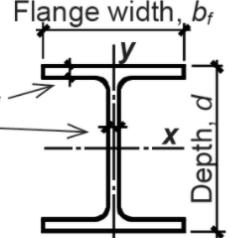
Table A-4.1: Steel properties¹

Category	ASTM designation	Yield stress, F_y (ksi)	(Ultimate) tensile stress, F_u (ksi)	Preferred for these shapes
Carbon	A36 A500 Gr. B A500 Gr. B A53 Gr. B	36 42 46 ² 35	58 58 58 60	M, S, C, MC, L, plates ⁴ and bars HSS round ⁵ HSS rectangular ⁵ Pipe
High-strength, low-alloy	A992 A572 Gr. 50	50 50	65 65	³ W HP

Notes:

1. The modulus of elasticity, E , for these steels can be taken as 29,000 ksi.

Table A-4.3: Dimensions and properties of steel W sections⁵



Cross-sectional area = A
 Moment of inertia = I
 Section modulus, $S_x = 2I_x/d$
 Sectional modulus, $S_y = 2I_y/b_f$
 Radius of gyration, $r_x = \sqrt{I_x/A}$
 Radius of gyration, $r_y = \sqrt{I_y/A}$

Designation	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W24 × 68 ⁴	20.1	23.7	0.415	8.97	0.585	154	177	1830	70.4	1.87
W24 × 76 ⁴	22.4	23.9	0.440	8.99	0.680	176	200	2100	82.5	1.92
W24 × 84 ⁴	24.7	24.1	0.470	9.02	0.770	196	224	2370	94.4	1.95
W24 × 94 ⁴	27.7	24.3	0.515	9.07	0.875	222	254	2700	109	1.98
W24 × 103 ⁴	30.3	24.5	0.550	9.00	0.980	245	280	3000	119	1.99

Chapter 4 — Steel: Appendix

Table A-4.1: Steel properties¹

Category	ASTM designation	Yield stress, F_y (ksi)	(Ultimate) tensile stress, F_u (ksi)	Preferred for these shapes
Carbon	A36	36	58	M, S, C, MC, L, plates ⁴ and bars
	A500 Gr. B	42	58	HSS round ⁵
	A500 Gr. B	46	58	HSS rectangular ⁵
	A53 Gr. B	35	60	Pipe
High-strength, low-alloy	A992	50	65	³ W
	A572 Gr. 50	50	65	HP

Notes:

1. The modulus of elasticity, E , for these steels can be taken as 29,000 ksi.

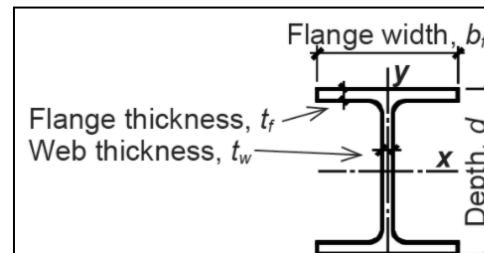
TOTAL LOAD DEFLECTION:

So, we can now compute the *actual* total load deflection:

$$\Delta = CP(L/12)^3 / (EI_x), \text{ or}$$

$$\Delta = (85.54)(29.12)(32)^3 / (29,000 \times 2100) = 1.34 \text{ in.}$$

Table A-4.3: Dimensions and properties of steel W sections⁵



Flange width, b_f
Flange thickness, t_f
Web thickness, t_w
Depth, d

Cross-sectional area = A
Moment of inertia = I
Section modulus, $S_x = 2I_x/d$
Sectional modulus, $S_y = 2I_y/b_f$
Radius of gyration, $r_x = \sqrt{I_x/A}$
Radius of gyration, $r_y = \sqrt{I_y/A}$

Designation	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W24 × 68 ⁴	20.1	23.7	0.415	8.97	0.585	154	177	1830	70.4	1.87
W24 × 76 ⁴	22.4	23.9	0.440	8.99	0.680	176	200	2100	82.5	1.92
W24 × 84 ⁴	24.7	24.1	0.470	9.02	0.770	196	224	2370	94.4	1.95
W24 × 94 ⁴	27.7	24.3	0.515	9.07	0.875	222	254	2700	109	1.98
W24 × 103 ⁴	30.3	24.5	0.550	9.00	0.980	245	280	3000	119	1.99

Chapter 4 — Steel: Appendix

Table A-4.1: Steel properties¹

Category	ASTM designation	Yield stress, F_y (ksi)	(Ultimate) tensile stress, F_u (ksi)	Preferred for these shapes
Carbon	A36 A500 Gr. B A500 Gr. B A53 Gr. B	36 42 46 235	58 58 58 60	M, S, C, MC, L, plates ⁴ and bars HSS round ⁵ HSS rectangular ⁵ Pipe
High-strength, low-alloy	A992 A572 Gr. 50	50 50	65 65	³ W HP

Notes:

1. The modulus of elasticity, E , for these steels can be taken as 29,000 ksi.

TOTAL LOAD DEFLECTION:

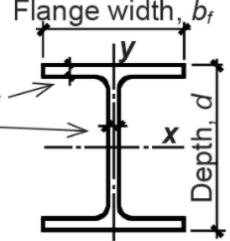
So, we can now compute the *actual* total load deflection:

$$\Delta = CP(L/12)^3 / (EI_x), \text{ or}$$

$$\Delta = (85.54)(29.12)(32)^3 / (29,000 \times 2100) = 1.34 \text{ in.}$$

The *allowable* total load deflection can be found in the footnotes to Table A-4.17 (or A-3.15):

Table A-4.3: Dimensions and properties of steel W sections⁵



Cross-sectional area = A
 Moment of inertia = I
 Section modulus, $S_x = 2I_x/d$
 Sectional modulus, $S_y = 2I_y/b_f$
 Radius of gyration, $r_x = \sqrt{I_x/A}$
 Radius of gyration, $r_y = \sqrt{I_y/A}$

Designation	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W24 × 68 ⁴	20.1	23.7	0.415	8.97	0.585	154	177	1830	70.4	1.87
W24 × 76 ⁴	22.4	23.9	0.440	8.99	0.680	176	200	2100	82.5	1.92
W24 × 84 ⁴	24.7	24.1	0.470	9.02	0.770	196	224	2370	94.4	1.95
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Chapter 4 — Steel: Appendix

Table A-4.1: Steel properties¹

Category	ASTM designation	Yield stress, F_y (ksi)	(Ultimate) tensile stress, F_u (ksi)	Preferred for these shapes
Carbon	A36	36	58	M, S, C, MC, L, plates ⁴ and bars
	A500 Gr. B	42	58	HSS round ⁵
	A500 Gr. B	46	58	HSS rectangular ⁵
	A53 Gr. B	35	60	Pipe
High-strength, low-alloy	A992	50	65	³ W
	A572 Gr. 50	50	65	HP

Notes:

1. The modulus of elasticity, E , for these steels can be taken as 29,000 ksi.

TOTAL LOAD DEFLECTION:

So, we can now compute the *actual* total load deflection:

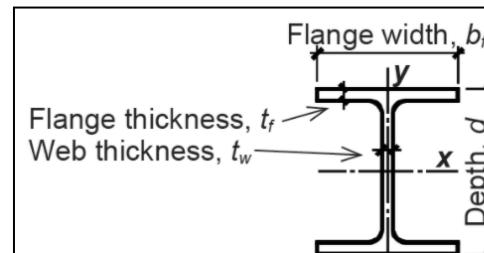
$$\Delta = CP(L/12)^3 / (EI_x), \text{ or}$$

$$\Delta = (85.54)(29.12)(32)^3 / (29,000 \times 2100) = 1.34 \text{ in.}$$

The *allowable* total load deflection can be found in the footnotes to Table A-4.17 (or A-3.15):

For total loads (combined live and dead), the typical basic floor beam limit is **L/240** while typical roof beam limits are *L/120*, *L/180*, or *L/240* (for no ceiling, nonplaster ceiling, or plaster ceiling respectively).

Table A-4.3: Dimensions and properties of steel W sections⁵



Cross-sectional area = A
 Moment of inertia = I
 Section modulus, $S_x = 2I_x/d$
 Sectional modulus, $S_y = 2I_y/b_f$
 Radius of gyration, $r_x = \sqrt{I_x/A}$
 Radius of gyration, $r_y = \sqrt{I_y/A}$

Designation	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W24 × 68 ⁴	20.1	23.7	0.415	8.97	0.585	154	177	1830	70.4	1.87
W24 × 76 ⁴	22.4	23.9	0.440	8.99	0.680	176	200	2100	82.5	1.92
W24 × 84 ⁴	24.7	24.1	0.470	9.02	0.770	196	224	2370	94.4	1.95
W24 × 94 ⁴	27.7	24.3	0.515	9.07	0.875	222	254	2700	109	1.98
W24 × 103 ⁴	30.3	24.5	0.550	9.00	0.980	245	280	3000	119	1.99

Chapter 4 — Steel: Appendix

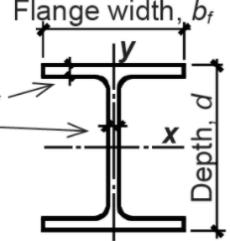
Table A-4.1: Steel properties¹

Category	ASTM designation	Yield stress, F_y (ksi)	(Ultimate) tensile stress, F_u (ksi)	Preferred for these shapes
Carbon	A36	36	58	M, S, C, MC, L, plates ⁴ and bars
	A500 Gr. B	42	58	HSS round ⁵
	A500 Gr. B	46	58	HSS rectangular ⁵
	A53 Gr. B	35	60	Pipe
High-strength, low-alloy	A992	50	65	³ W
	A572 Gr. 50	50	65	HP

Notes:

1. The modulus of elasticity, E , for these steels can be taken as 29,000 ksi.

Table A-4.3: Dimensions and properties of steel W sections⁵



Cross-sectional area = A
 Moment of inertia = I
 Section modulus, $S_x = 2I_x/d$
 Sectional modulus, $S_y = 2I_y/b_f$
 Radius of gyration, $r_x = \sqrt{I_x/A}$
 Radius of gyration, $r_y = \sqrt{I_y/A}$

Designation	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W24 × 68 ⁴	20.1	23.7	0.415	8.97	0.585	154	177	1830	70.4	1.87
W24 × 76 ⁴	22.4	23.9	0.440	8.99	0.680	176	200	2100	82.5	1.92
W24 × 84 ⁴	24.7	24.1	0.470	9.02	0.770	196	224	2370	94.4	1.95
W24 × 94 ⁴	27.7	24.3	0.515	9.07	0.875	222	254	2700	109	1.98
W24 × 103 ⁴	30.3	24.5	0.550	9.00	0.980	245	280	3000	119	1.99

TOTAL LOAD DEFLECTION:

So, we can now compute the *actual* total load deflection:

$$\Delta = CP(L/12)^3 / (EI_x), \text{ or}$$

$$\Delta = (85.54)(29.12)(32)^3 / (29,000 \times 2100) = 1.34 \text{ in.}$$

The *allowable* total load deflection can be found in the footnotes to Table A-4.17 (or A-3.15):

For total loads (combined live and dead), the typical basic floor beam limit is **L/240** while typical roof beam limits are *L/120*, *L/180*, or *L/240* (for no ceiling, nonplaster ceiling, or plaster ceiling respectively).

Using the typical limit of L/240 (with *L* expressed in inches), we get an allowable value of $32 \times 12 / 240 = 1.6 \text{ in.}$

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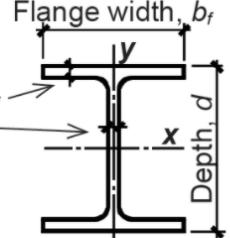
Table A-4.1: Steel properties¹

Category	ASTM designation	Yield stress, F_y (ksi)	(Ultimate) tensile stress, F_u (ksi)	Preferred for these shapes
Carbon	A36	36	58	M, S, C, MC, L, plates ⁴ and bars
	A500 Gr. B	42	58	HSS round ⁵
	A500 Gr. B	46	58	HSS rectangular ⁵
	A53 Gr. B	235	60	Pipe
High-strength, low-alloy	A992	50	65	³ W
	A572 Gr. 50	50	65	HP

Notes:

1. The modulus of elasticity, E , for these steels can be taken as 29,000 ksi.

Table A-4.3: Dimensions and properties of steel W sections⁵



Flange width, b_f
Flange thickness, t_f
Web thickness, t_w
Depth, d

Cross-sectional area = A
Moment of inertia = I
Section modulus, $S_x = 2I_x/d$
Sectional modulus, $S_y = 2I_y/b_f$
Radius of gyration, $r_x = \sqrt{I_x/A}$
Radius of gyration, $r_y = \sqrt{I_y/A}$

Designation	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W24 × 68 ⁴	20.1	23.7	0.415	8.97	0.585	154	177	1830	70.4	1.87
W24 × 76 ⁴	22.4	23.9	0.440	8.99	0.680	176	200	2100	82.5	1.92
W24 × 84 ⁴	24.7	24.1	0.470	9.02	0.770	196	224	2370	94.4	1.95
W24 × 94 ⁴	27.7	24.3	0.515	9.07	0.875	222	254	2700	109	1.98
W24 × 103 ⁴	30.3	24.5	0.550	9.00	0.980	245	280	3000	119	1.99

TOTAL LOAD DEFLECTION:

So, we can now compute the *actual* total load deflection:

$$\Delta = CP(L/12)^3 / (EI_x), \text{ or}$$

$$\Delta = (85.54)(29.12)(32)^3 / (29,000 \times 2100) = 1.34 \text{ in.}$$

The *allowable* total load deflection can be found in the footnotes to Table A-4.17 (or A-3.15):

For total loads (combined live and dead), the typical basic floor beam limit is **L/240** while typical roof beam limits are *L/120*, *L/180*, or *L/240* (for no ceiling, nonplaster ceiling, or plaster ceiling respectively).

Using the typical limit of L/240 (with *L* expressed in inches), we get an allowable value of $32 \times 12 / 240 = 1.6 \text{ in.}$

Conclusion: Since the actual total-load deflection is less than or equal to the allowable total-load deflection, the W24x76 is OK for total-load deflection!

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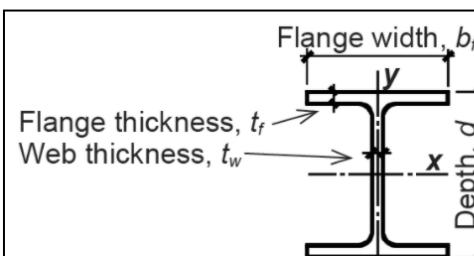
Table A-4.1: Steel properties¹

Category	ASTM designation	Yield stress, F_y (ksi)	(Ultimate) tensile stress, F_u (ksi)	Preferred for these shapes
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	A500 Gr. B	42	58	HSS round ⁵
	A500 Gr. B	46	58	HSS rectangular ⁵
	A53 Gr. B	35	60	Pipe
High-strength, low-alloy	A992	50	65	³ W
	A572 Gr. 50	50	65	HP

Notes:

1. The modulus of elasticity, E , for these steels can be taken as 29,000 ksi.

Table A-4.3: Dimensions and properties of steel W sections⁵



Designation	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W24 × 68 ⁴	20.1	23.7	0.415	8.97	0.585	154	177	1830	70.4	1.87
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W24 × 103 ⁴	30.3	24.5	0.550	9.00	0.980	245	280	3000	119	1.99

LIVE LOAD DEFLECTION:

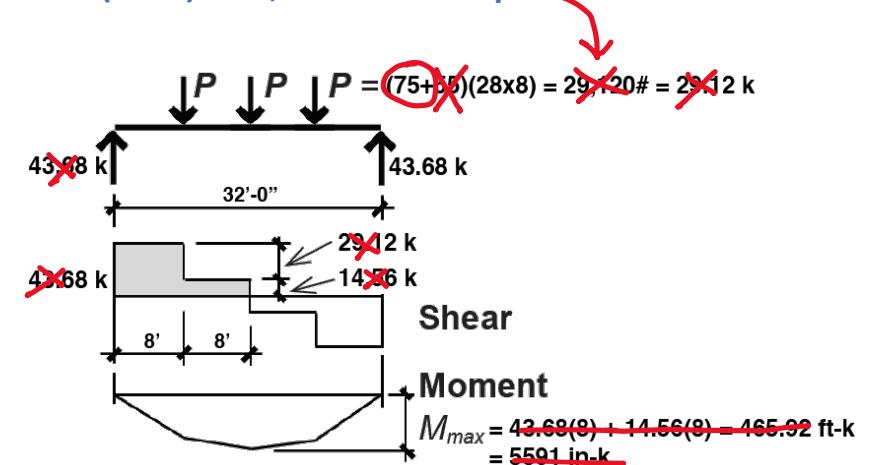
So, we can now compute the *actual* live load deflection:

$$\Delta = CP(L/12)^3 / (EI_x), \text{ or}$$

$$\Delta = (85.54)(16.8)(32)^3 / (29,000 \times 2100) = 0.77 \text{ in.}$$

To find the concentrated load, P , for live load only:

$$P = 75(28 \times 8) = 16,800\# = 16.8 \text{ kips}$$



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Table A-4.1: Steel properties¹

Category	ASTM designation	Yield stress, F_y (ksi)	(Ultimate) tensile stress, F_u (ksi)	Preferred for these shapes
Carbon	A36	36	58	M, S, C, MC, L, plates ⁴ and bars
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High-strength, low-alloy	A992	50	65	³ W
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Notes:

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LIVE LOAD DEFLECTION:

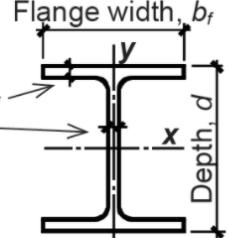
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The *allowable* total load deflection can be found in the footnotes to Table A-4.17 (or A-3.15):

Table A-4.3: Dimensions and properties of steel W sections⁵



Flange width, b_f
Flange thickness, t_f
Web thickness, t_w
Depth, d

Cross-sectional area = A
Moment of inertia = I
Section modulus, $S_x = 2I_x/d$
Sectional modulus, $S_y = 2I_y/b_f$
Radius of gyration, $r_x = \sqrt{I_x/A}$
Radius of gyration, $r_y = \sqrt{I_y/A}$

Designation	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W24 × 68 ⁴	20.1	23.7	0.415	8.97	0.585	154	177	1830	70.4	1.87
W24 × 76 ⁴	22.4	23.9	0.440	8.99	0.680	176	200	2100	82.5	1.92
W24 × 84 ⁴	24.7	24.1	0.470	9.02	0.770	196	224	2370	94.4	1.95
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W24 × 103 ⁴	30.3	24.5	0.550	9.00	0.980	245	280	3000	119	1.99

Chapter 4 — Steel: Appendix

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Notes:

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LIVE LOAD DEFLECTION:

So, we can now compute the *actual* live load deflection:

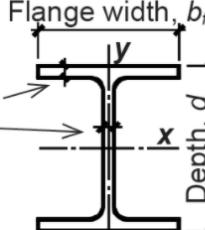
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The *allowable* total load deflection can be found in the footnotes to Table A-4.17 (or A-3.15):

For total loads (combined live and dead), the typical basic floor beam limit is **L/360** while typical roof beam limits are $L/180$, $L/240$, or $L/360$ (for no ceiling, nonplaster ceiling, or plaster ceiling respectively).

Table A-4.3: Dimensions and properties of steel W sections⁵



Cross-sectional area = A
 Moment of inertia = I
 Section modulus, $S_x = 2I_x/d$
 Sectional modulus, $S_y = 2I_y/b_f$
 Radius of gyration, $r_x = \sqrt{I_x/A}$
 Radius of gyration, $r_y = \sqrt{I_y/A}$

Designation	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W24 × 68 ⁴	20.1	23.7	0.415	8.97	0.585	154	177	1830	70.4	1.87
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W24 × 84 ⁴	24.7	24.1	0.470	9.02	0.770	196	224	2370	94.4	1.95
W24 × 94 ⁴	27.7	24.3	0.515	9.07	0.875	222	254	2700	109	1.98
W24 × 103 ⁴	30.3	24.5	0.550	9.00	0.980	245	280	3000	119	1.99

Chapter 4 — Steel: Appendix

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High-strength, low-alloy	A992	50	65	³ W
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Notes:

1. The modulus of elasticity, E , for these steels can be taken as 29,000 ksi.

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Designation	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
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LIVE LOAD DEFLECTION:

So, we can now compute the *actual* live load deflection:

$$\Delta = CP(L/12)^3 / (EI_x), \text{ or}$$

$$\Delta = (85.54)(16.8)(32)^3 / (29,000 \times 2100) = 0.77 \text{ in.}$$

The *allowable* total load deflection can be found in the footnotes to Table A-4.17 (or A-3.15):

For total loads (combined live and dead), the typical basic floor beam limit is **L/360** while typical roof beam limits are $L/180$, $L/240$, or $L/360$ (for no ceiling, nonplaster ceiling, or plaster ceiling respectively).

Using the typical limit of L/360 (with L expressed in inches), we get an allowable value of $32 \times 12 / 360 = 1.07 \text{ in.}$

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Table A-4.1: Steel properties¹

Category	ASTM designation	Yield stress, F_y (ksi)	(Ultimate) tensile stress, F_u (ksi)	Preferred for these shapes
Carbon	A36 A500 Gr. B A500 Gr. B A53 Gr. B	36 42 46 235	58 58 58 60	M, S, C, MC, L, plates ⁴ and bars HSS round ⁵ HSS rectangular ⁵ Pipe
High-strength, low-alloy	A992 A572 Gr. 50	50 50	65 65	³ W HP

Notes:

1. The modulus of elasticity, E , for these steels can be taken as 29,000 ksi.

Table A-4.3: Dimensions and properties of steel W sections⁵

Flange width, b_f
Flange thickness, t_f
Web thickness, t_w
Depth, d

Cross-sectional area = A
Moment of inertia = I
Section modulus, $S_x = 2I_x/d$
Sectional modulus, $S_y = 2I_y/b_f$
Radius of gyration, $r_x = \sqrt{I_x/A}$
Radius of gyration, $r_y = \sqrt{I_y/A}$

Designation	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W24 × 68 ⁴	20.1	23.7	0.415	8.97	0.585	154	177	1830	70.4	1.87
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W24 × 84 ⁴	24.7	24.1	0.470	9.02	0.770	196	224	2370	94.4	1.95
W24 × 94 ⁴	27.7	24.3	0.515	9.07	0.875	222	254	2700	109	1.98
W24 × 103 ⁴	30.3	24.5	0.550	9.00	0.980	245	280	3000	119	1.99

LIVE LOAD DEFLECTION:

So, we can now compute the *actual* live load deflection:

$$\Delta = CP(L/12)^3 / (EI_x), \text{ or}$$

$$\Delta = (85.54)(16.8)(32)^3 / (29,000 \times 2100) = 0.77 \text{ in.}$$

The *allowable* total load deflection can be found in the footnotes to Table A-4.17 (or A-3.15):

For total loads (combined live and dead), the typical basic floor beam limit is **L/360** while typical roof beam limits are $L/180$, $L/240$, or $L/360$ (for no ceiling, nonplaster ceiling, or plaster ceiling respectively).

Using the typical limit of L/360 (with L expressed in inches), we get an allowable value of $32 \times 12 / 360 = 1.07 \text{ in.}$

Conclusion: Since the actual live-load deflection is less than or equal to the allowable live-load deflection, the W24x76 is OK for live-load deflection!

Chapter 4 — Steel: Appendix

Table A-4.1: Steel properties¹

Category	ASTM designation	Yield stress, F_y (ksi)	(Ultimate) tensile stress, F_u (ksi)	Preferred for these shapes
Carbon	A36 A500 Gr. B A500 Gr. B A53 Gr. B	36 42 46 235	58 58 58 60	M, S, C, MC, L, plates ⁴ and bars HSS round ⁵ HSS rectangular ⁵ Pipe
High-strength, low-alloy	A992 A572 Gr. 50	50 50	65 65	³ W HP

Notes:

1. The modulus of elasticity, E , for these steels can be taken as 29,000 ksi.

Table A-4.3: Dimensions and properties of steel W sections⁵

Flange width, b_f
Flange thickness, t_f
Web thickness, t_w
Depth, d

Cross-sectional area = A
Moment of inertia = I
Section modulus, $S_x = 2I_x/d$
Sectional modulus, $S_y = 2I_y/b_f$
Radius of gyration, $r_x = \sqrt{I_x/A}$
Radius of gyration, $r_y = \sqrt{I_y/A}$

Designation	A (in ²)	d (in.)	t_w (in.)	b_f (in.)	t_f (in.)	S_x (in ³)	Z_x (in ³)	I_x (in ⁴)	I_y (in ⁴)	r_y (in.)
W24 × 68 ⁴	20.1	23.7	0.415	8.97	0.585	154	177	1830	70.4	1.87
W24 × 76 ⁴	22.4	23.9	0.440	8.99	0.680	176	200	2100	82.5	1.92
W24 × 84 ⁴	24.7	24.1	0.470	9.02	0.770	196	224	2370	94.4	1.95
W24 × 94 ⁴	27.7	24.3	0.515	9.07	0.875	222	254	2700	109	1.98
W24 × 103 ⁴	30.3	24.5	0.550	9.00	0.980	245	280	3000	119	1.99

LIVE LOAD DEFLECTION:

So, we can now compute the *actual* live load deflection:

$$\Delta = CP(L/12)^3 / (EI_x), \text{ or}$$

$$\Delta = (85.54)(16.8)(32)^3 / (29,000 \times 2100) = 0.77 \text{ in.}$$

The *allowable* total load deflection can be found in the footnotes to Table A-4.17 (or A-3.15):

For total loads (combined live and dead), the typical basic floor beam limit is **L/360** while typical roof beam limits are $L/180$, $L/240$, or $L/360$ (for no ceiling, nonplaster ceiling, or plaster ceiling respectively).

Using the typical limit of L/360 (with L expressed in inches), we get an allowable value of $32 \times 12 / 360 = 1.07 \text{ in.}$

Conclusion: Since the actual live-load deflection is less than or equal to the allowable live-load deflection, the W24x76 is OK for live-load deflection!

Conclusion: The W24x76 is good for bending, shear, and deflection, so it works!